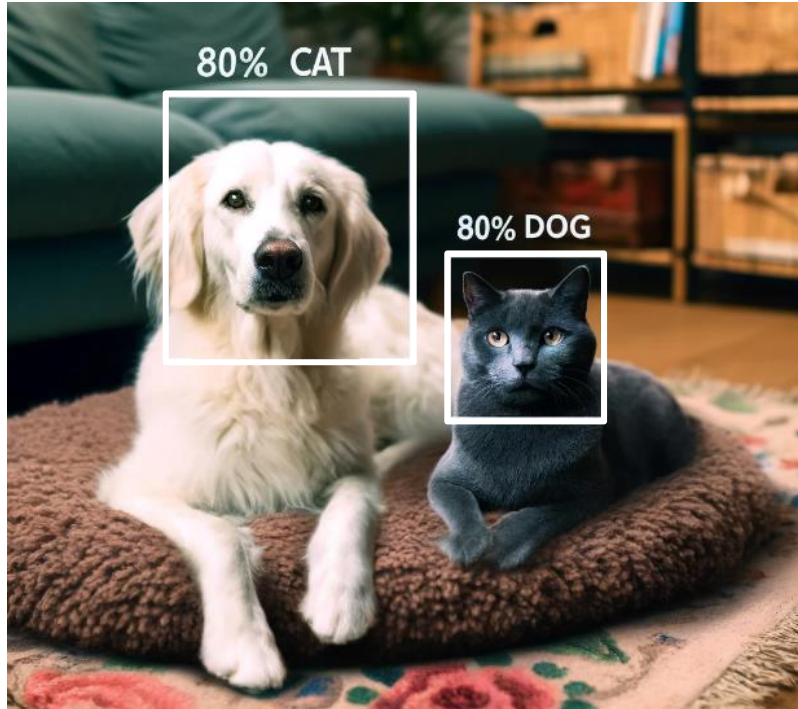


# Cost-Sensitive Uncertainty-Based Failure Recognition for Object Detection

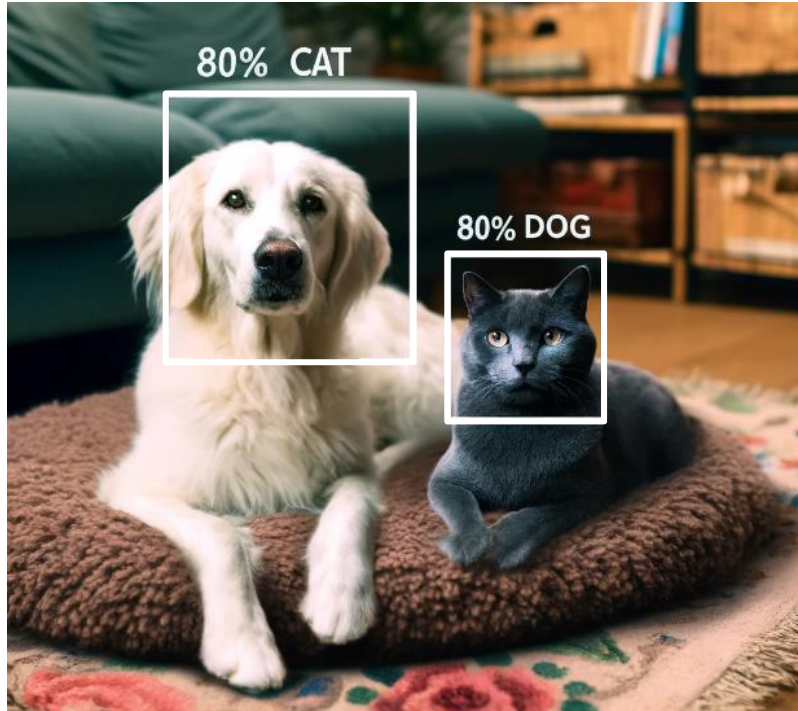
Moussa Kassem Sbeyti, Michelle Karg, Christian Wirth, Nadja Klein, and Sahin Albayrak

# Motivation

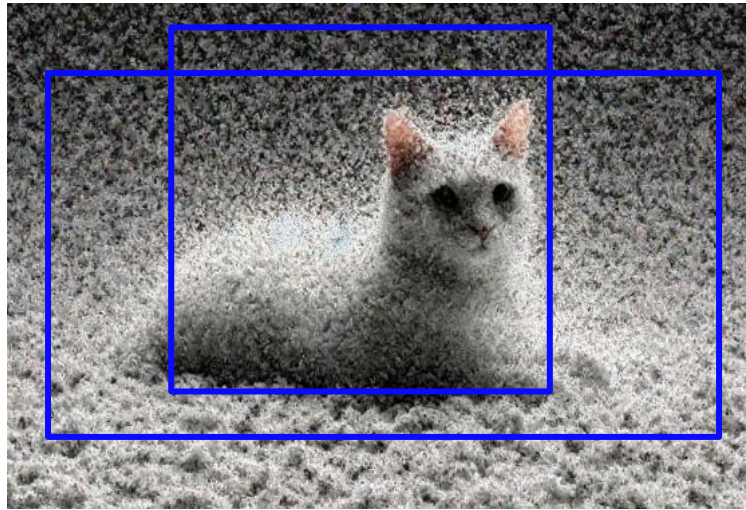


Over/underconfidence

# Motivation

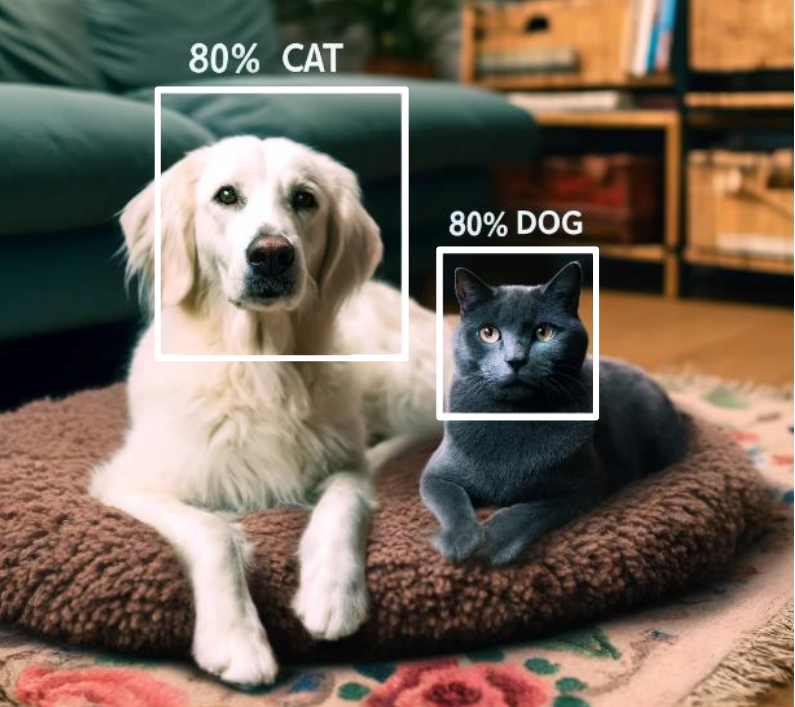


Over/underconfidence

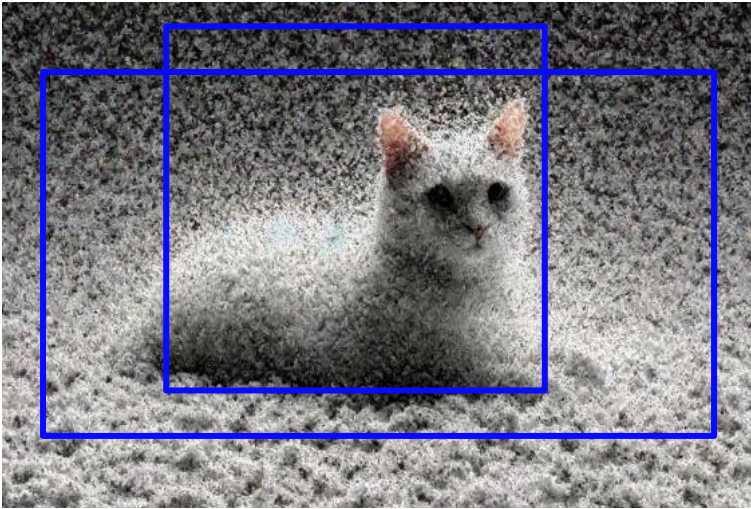


Noisy objects

# Motivation



Over/underconfidence

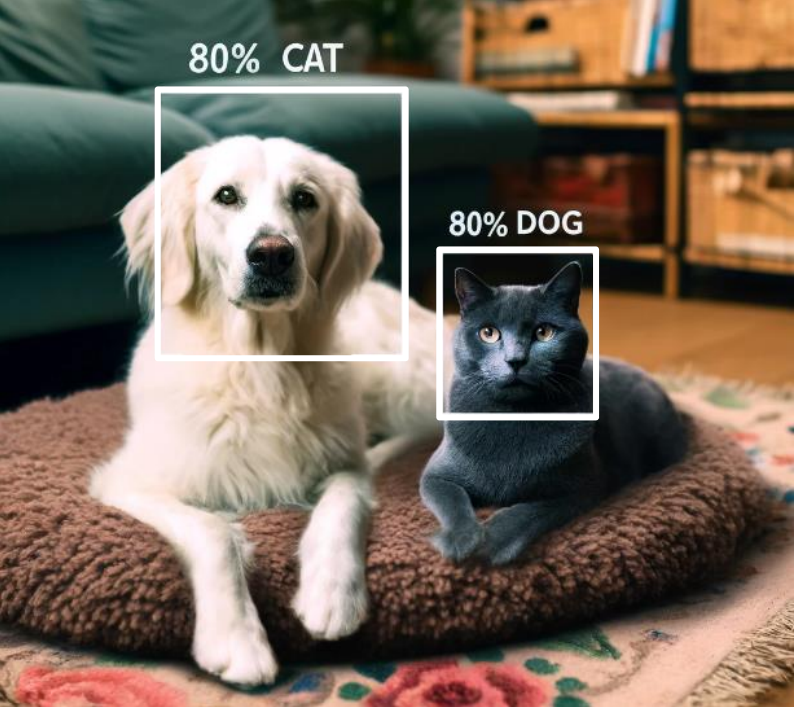


Noisy objects

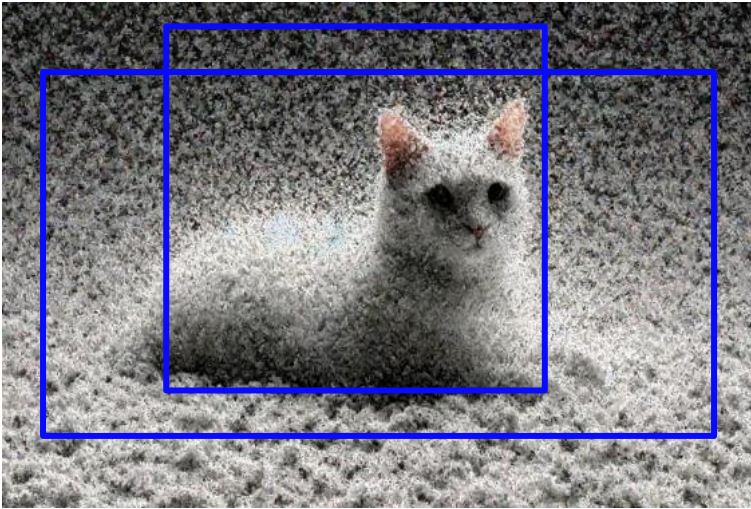


Unknown objects

# Motivation



Over/underconfidence



Noisy objects

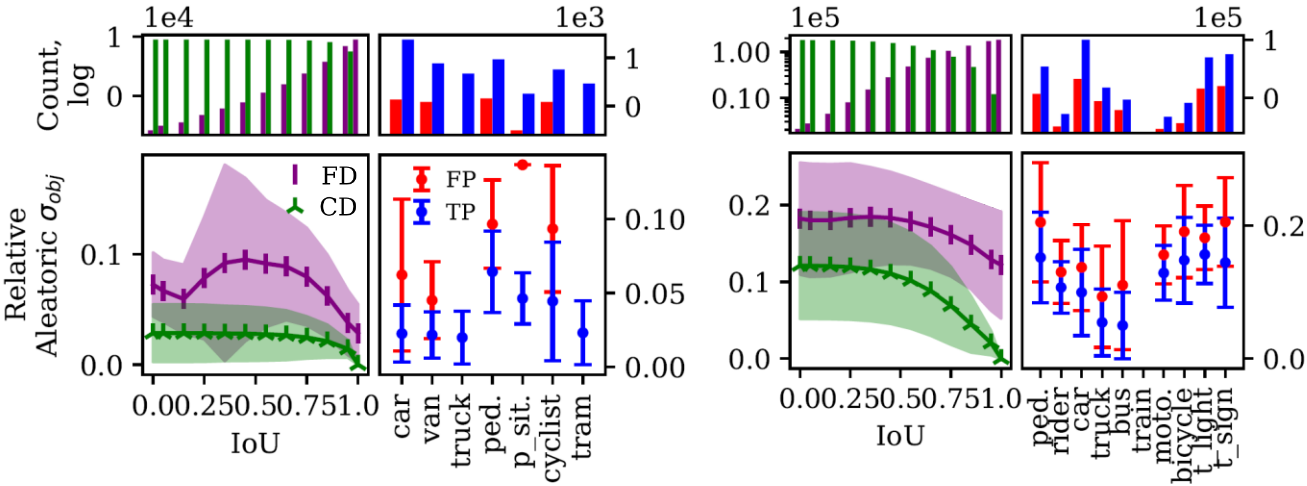


Unknown objects

*Reject option based on different uncertainties is required*

# I. Cost Sensitivity

Correlation Uncertainty vs Failures

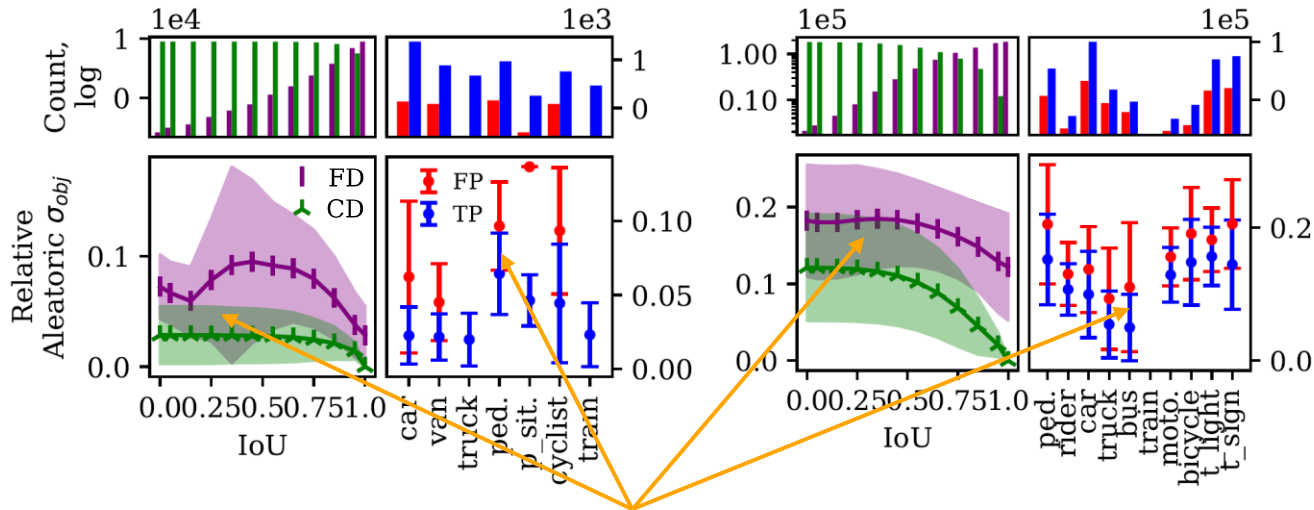


CD: Correct Detection  
 FD: False Detection  
 MD: Missing Detection

[1]

# I. Cost Sensitivity

Correlation Uncertainty vs Failures



*Challenge I: Overlap  $\Leftrightarrow$  Cost*

CD: Correct Detection

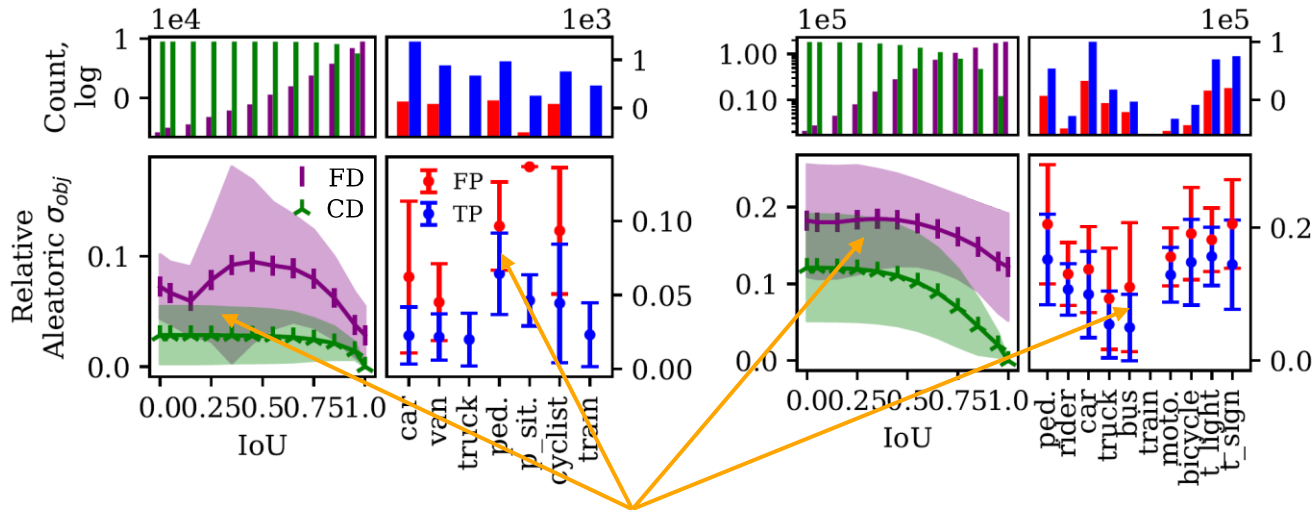
FD: False Detection

MD: Missing Detection

[1]

# I. Cost Sensitivity

Correlation Uncertainty vs Failures



*Challenge I: Overlap  $\Leftrightarrow$  Cost*

CD: Correct Detection  
 FD: False Detection  
 MD: Missing Detection

## Cost-Sensitive Approach

Table 1: Cost-matrix for detection thresholding.

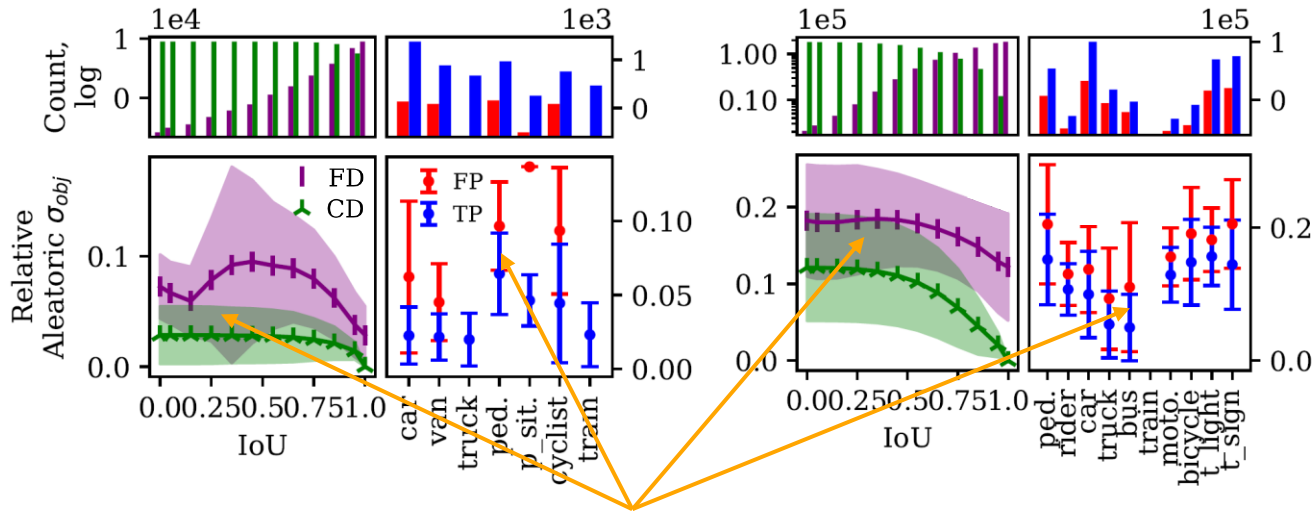
	CD	FD
CD <sub>T</sub>	$C_{CD} \cdot  CD $	$C_{FD} \cdot  FD $
FD <sub>T</sub>	$C_{MD} \cdot  MD $	$C_{BG} \cdot  BG $

[1]



# I. Cost Sensitivity

Correlation Uncertainty vs Failures



*Challenge I: Overlap  $\Leftrightarrow$  Cost*

CD: Correct Detection  
 FD: False Detection  
 MD: Missing Detection

## Cost-Sensitive Approach

Table 1: Cost-matrix for detection thresholding.

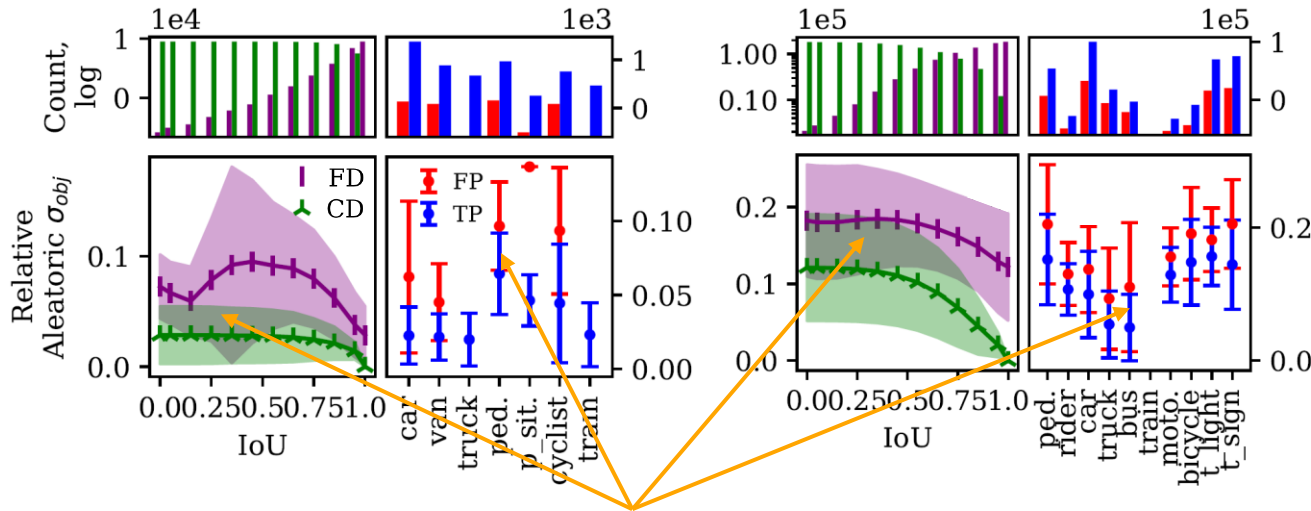
	CD	FD
CD <sub>T</sub>	0	$C_{FD} \cdot  FD $
FD <sub>T</sub>	$C_{MD} \cdot  MD $	0

$$C_{total} = C_{MD} \cdot |MD| + C_{FD} \cdot |FD|$$

[1]

# I. Cost Sensitivity

Correlation Uncertainty vs Failures



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	CD	FD
CD <sub>T</sub>	0	$C_{FD} \cdot  FD $
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$$C_{total} = C_{MD} \cdot |MD| + C_{FD} \cdot |FD|$$

Thresholding

Budget  $b \in [0, 1]$

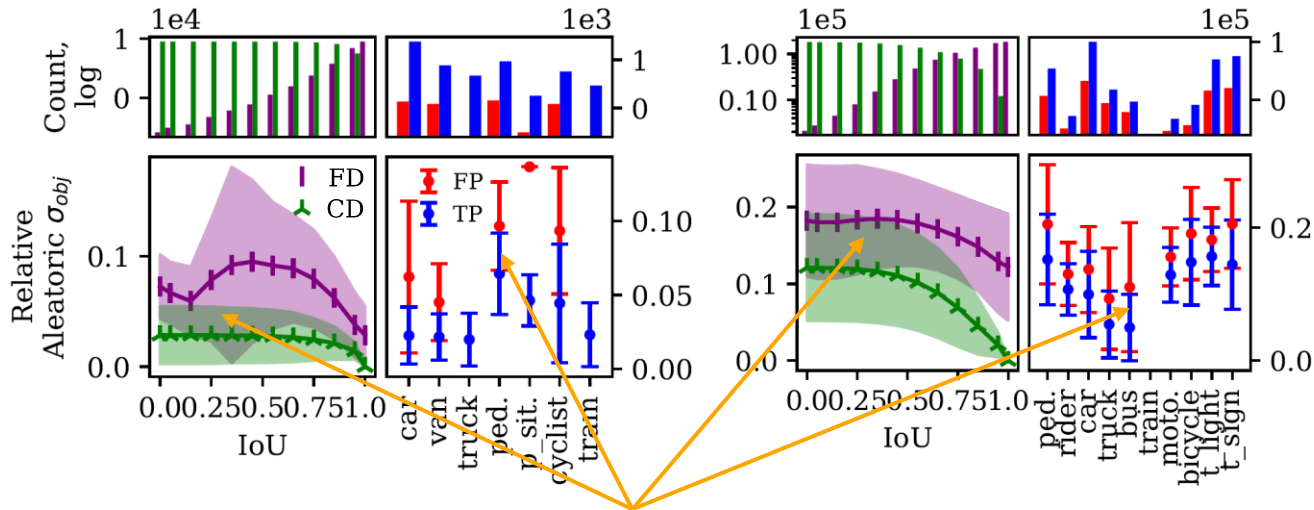
|CD|  
Before

|FD|  
Before

[1]

# I. Cost Sensitivity

Correlation Uncertainty vs Failures



**Challenge I: Overlap  $\Leftrightarrow$  Cost**

CD: Correct Detection  
 FD: False Detection  
 MD: Missing Detection

*Introduce cost-sensitivity into the detector*

## Cost-Sensitive Approach

Table 1: Cost-matrix for detection thresholding.

	CD	FD
CD <sub>T</sub>	0	$C_{FD} \cdot  FD $
FD <sub>T</sub>	$C_{MD} \cdot  MD $	0

$$C_{total} = C_{MD} \cdot |MD| + C_{FD} \cdot |FD|$$

### Thresholding

Budget  $b \in [0, 1]$

|CD|  
Before

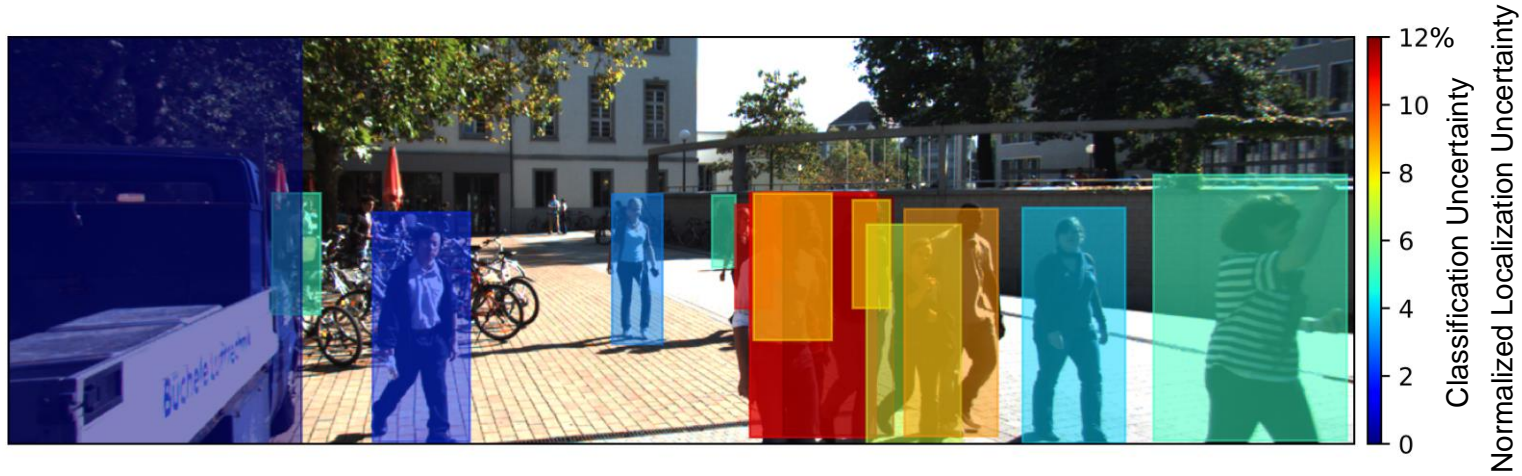
$b \cdot |CD|$   
After

|FD|  
Before

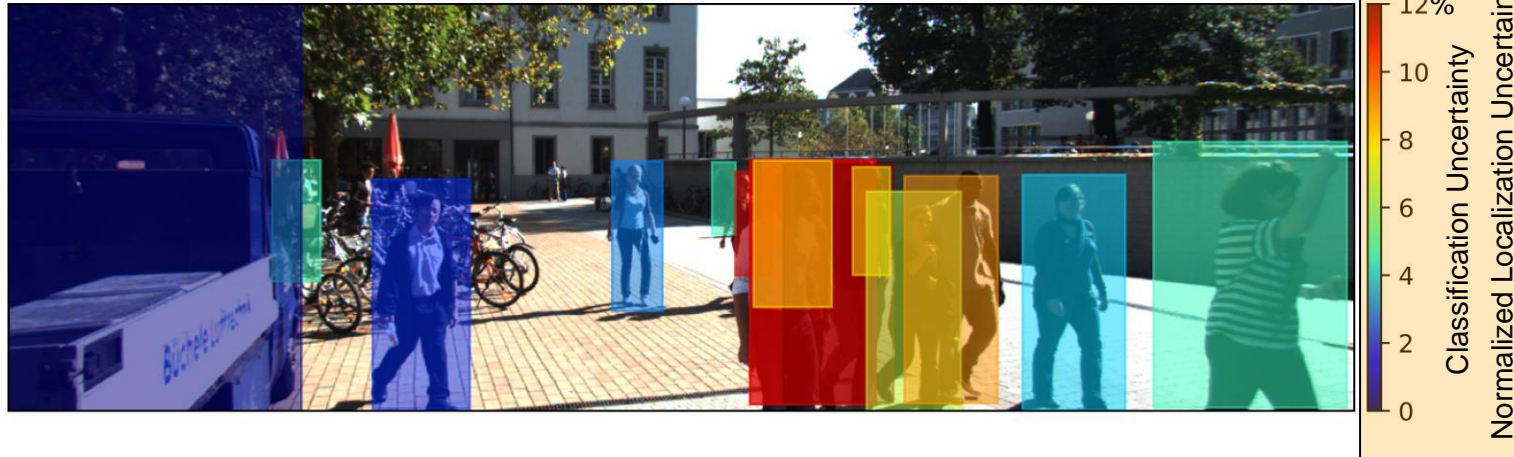
$b \cdot |FD|$   
After

[1]

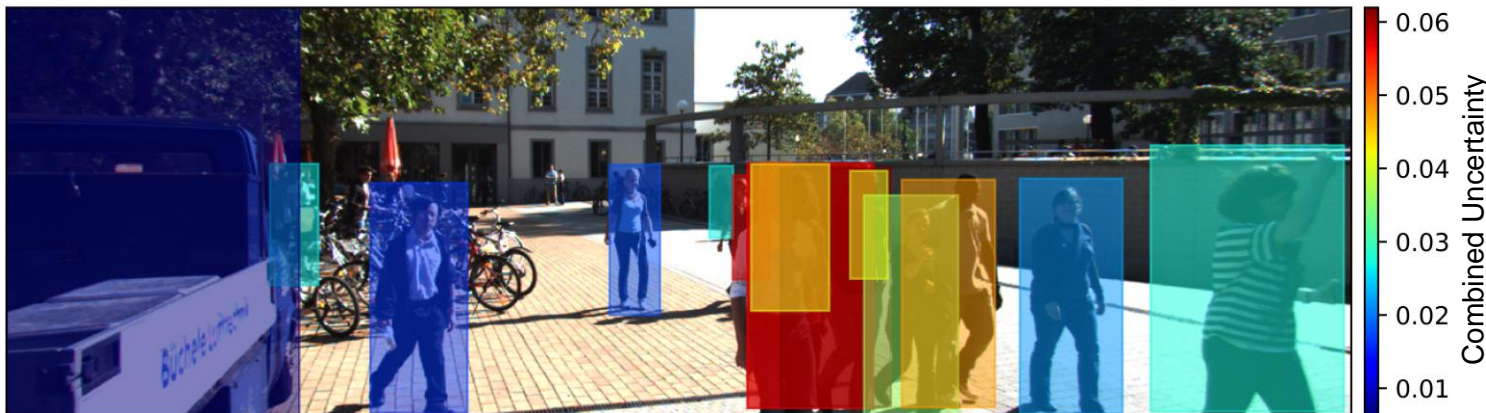
# II. Uncertainty-Based Thresholding



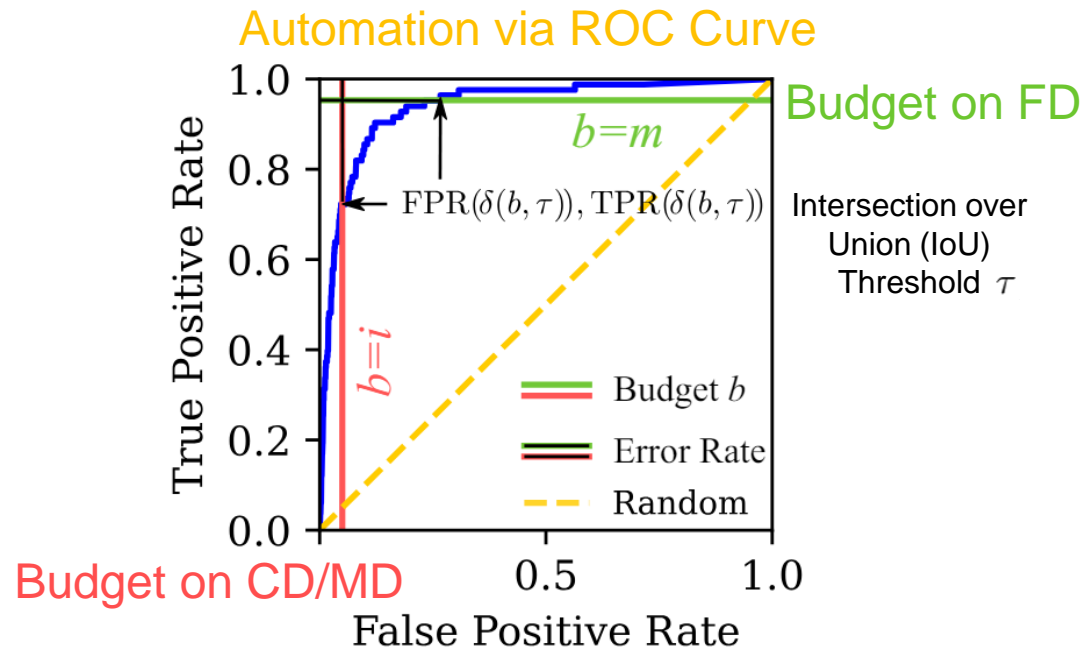
# II. Uncertainty-Based Thresholding



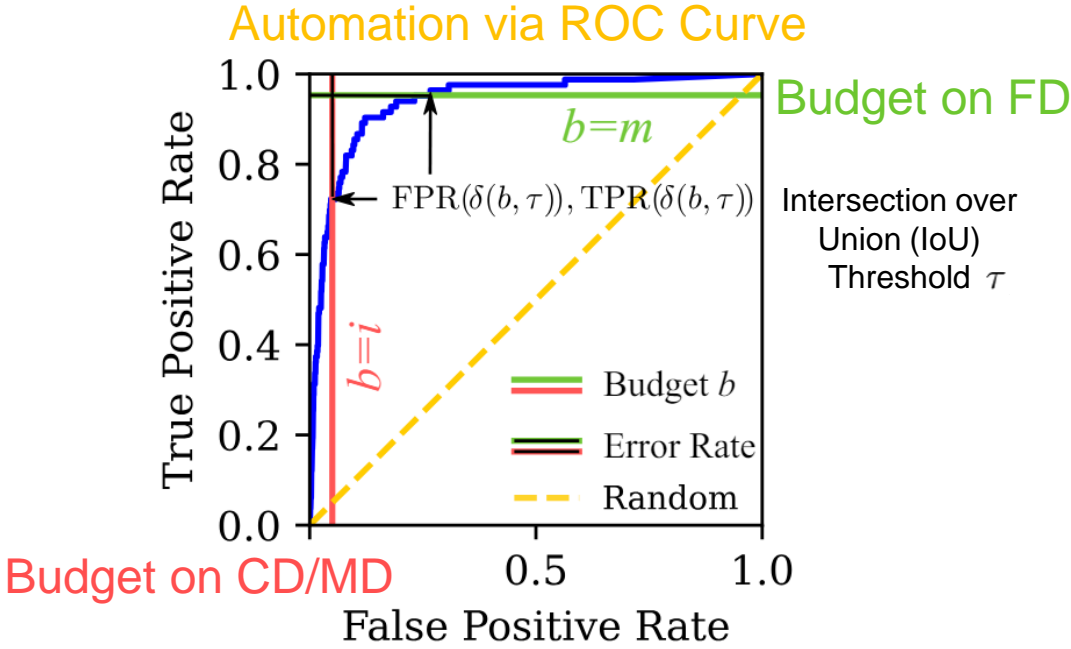
**Challenge II:**  
Selecting a threshold on  
uncertainty  $\in [0, \infty)$



# II. Uncertainty-Based Thresholding



# II. Uncertainty-Based Thresholding



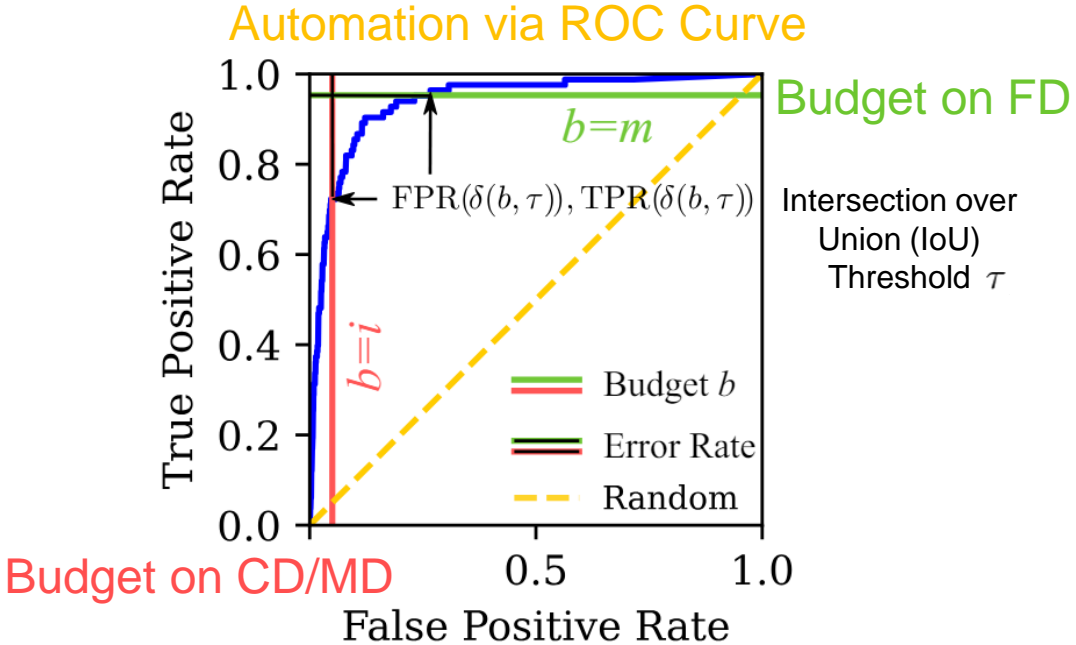
## Thresholding Performance

$$CD@FD(b) = \sum_{\tau=0.5}^{0.75} TNR(TPR(\delta(b, \tau)))$$

$$FD@CD(b) = \sum_{\tau=0.5}^{0.75} TPR(FPR(\delta(b, \tau)))$$

[2]

# II. Uncertainty-Based Thresholding



## Thresholding Performance

$$CD@FD(b) = \sum_{\tau=0.5}^{0.75} TNR(TPR(\delta(b, \tau)))$$

$$FD@CD(b) = \sum_{\tau=0.5}^{0.75} TPR(FPR(\delta(b, \tau)))$$

## Detector Performance

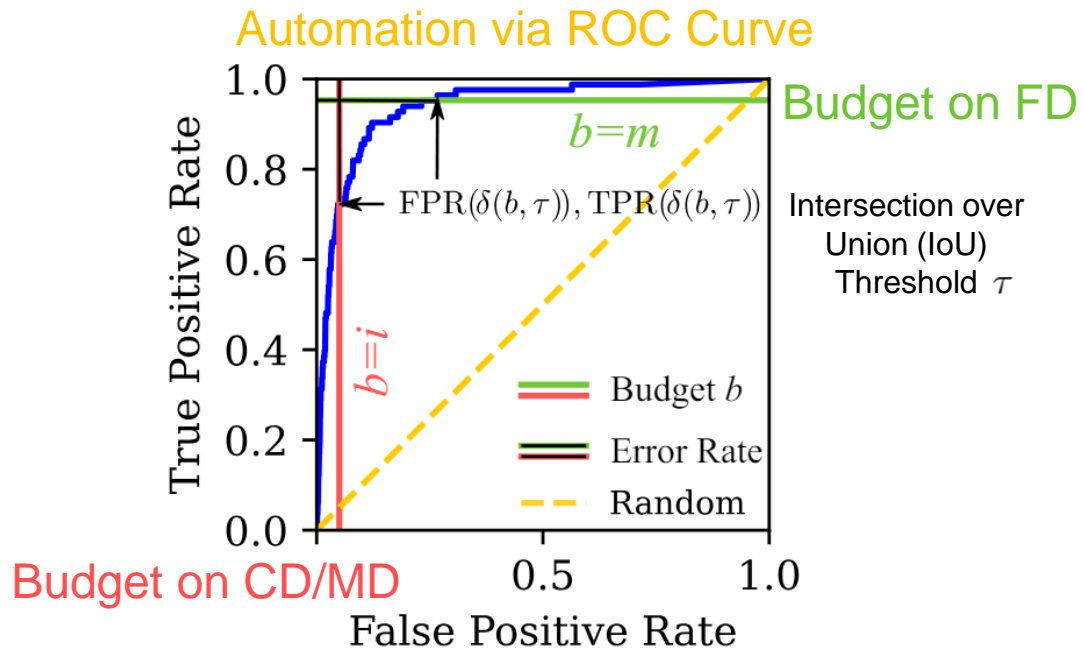
$$\frac{|CD|}{|CD| + |FD|} \leq \frac{i|CD|}{i|CD| + (1 - m)|FD|}$$

Recall, Precision, Accuracy, F1-Score

[2]



# II. Uncertainty-Based Thresholding



*Automate thresholding and its evaluation*

## Thresholding Performance

$$\text{CD@FD}(b) = \sum_{\tau=0.5}^{0.75} \text{TNR}(\text{TPR}(\delta(b, \tau)))$$

$$\text{FD@CD}(b) = \sum_{\tau=0.5}^{0.75} \text{TPR}(\text{FPR}(\delta(b, \tau)))$$

## Detector Performance

$$\frac{|\text{CD}|}{|\text{CD}| + |\text{FD}|} \leq \frac{i|\text{CD}|}{i|\text{CD}| + (1 - m)|\text{FD}|}$$

Recall, Precision, Accuracy, F1-Score

## Requirements

$$\text{minimize } \{(1 - i), 0\}$$

$$1 - i \leq m$$

$$(1 - i)(|\text{FD}| + |\text{CD}| + |\text{MD}|) \leq m|\text{FD}|$$

# III. Optimal Uncertainty Combination

Weights

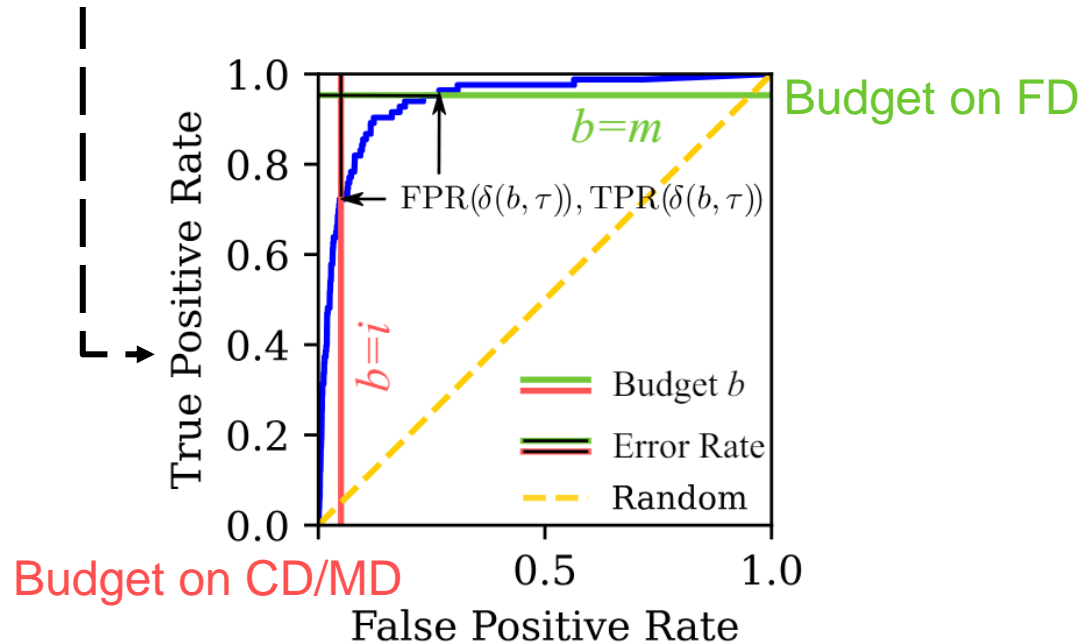
$$\mathbf{w}^\top \times (\sigma_{\text{cls}}, \sigma_{\text{loc}})^\top, \mathbf{w} = (w_1, w_2)^\top \in [0, 1]^2$$

*Challenge III: Optimal  
Combination*

# III. Optimal Uncertainty Combination

Weights

$$\mathbf{w}^\top \times (\sigma_{\text{cls}}, \sigma_{\text{loc}})^\top, \mathbf{w} = (w_1, w_2)^\top \in [0, 1]^2$$



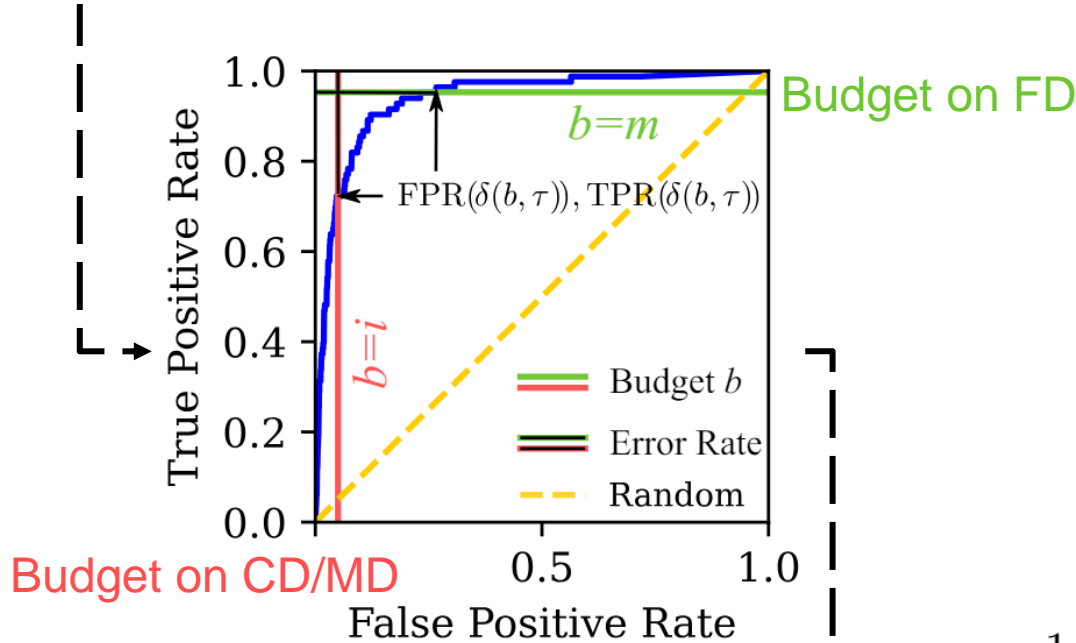
*Challenge III: Optimal Combination*

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*Challenge III: Optimal Combination*



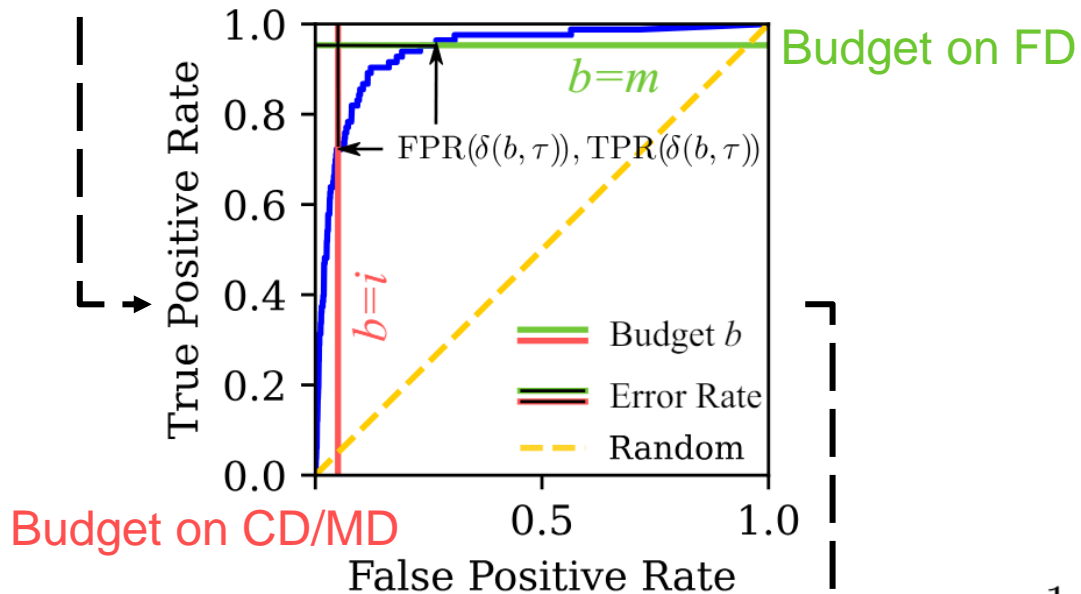
$$\mathcal{L}_{opt} = \frac{1}{6} \sum_{\tau \in \mathcal{T}} \begin{cases} \mathcal{L}_{step} = FNR(\delta_{opt}(b, \tau)) & \text{if } b = i \\ \mathcal{L}_{step} = FPR(\delta_{opt}(b, \tau)) & \text{if } b = m \end{cases}$$

$$\mathcal{T} = \{0.5, 0.55, 0.6, 0.65, 0.7, 0.75\}$$

# III. Optimal Uncertainty Combination

Weights

$$\rightarrow \mathbf{w}^\top \times (\sigma_{\text{cls}}, \sigma_{\text{loc}})^\top, \mathbf{w} = (w_1, w_2)^\top \in [0, 1]^2$$



**Challenge III: Optimal Combination**

**Black-Box Optimization**

For a given **budget**:

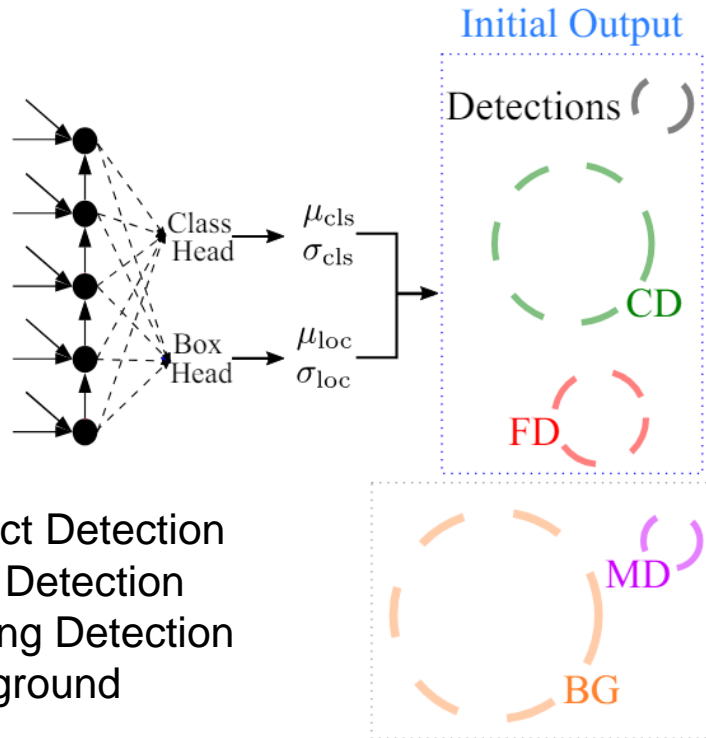
*Optimize the threshold and weights for the combined sum of the uncertainties over multiple IoU Thresholds*

$$\mathcal{L}_{opt} = \frac{1}{6} \sum_{\tau \in \mathcal{T}} \begin{cases} \mathcal{L}_{step} = FNR(\delta_{opt}(b, \tau)) & \text{if } b = i \\ \mathcal{L}_{step} = FPR(\delta_{opt}(b, \tau)) & \text{if } b = m \end{cases}$$

$$\mathcal{T} = \{0.5, 0.55, 0.6, 0.65, 0.7, 0.75\}$$

# Cost-Sensitive Uncertainty-Based Failure Recognition for Object Detection

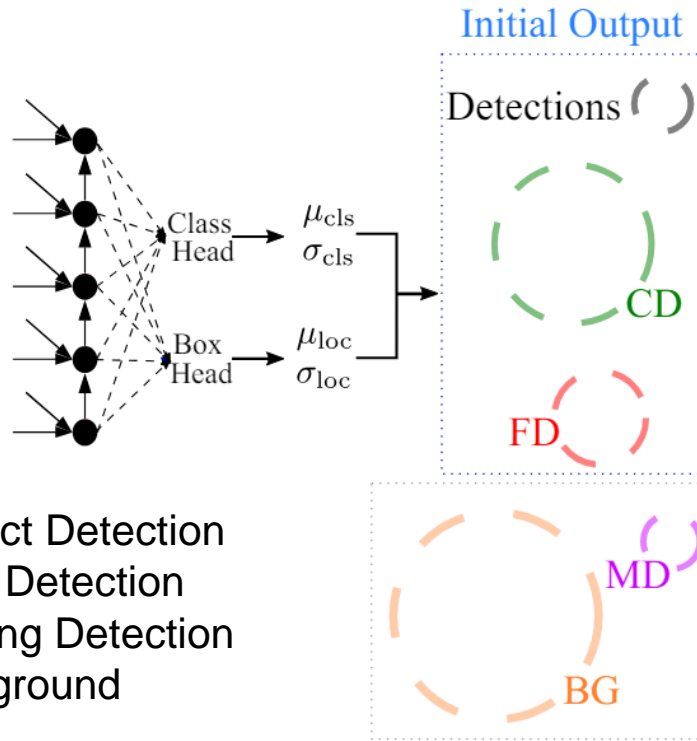
## I- Probabilistic Detector Output



CD: Correct Detection  
FD: False Detection  
MD: Missing Detection  
BG: Background

# Cost-Sensitive Uncertainty-Based Failure Recognition for Object Detection

## I- Probabilistic Detector Output

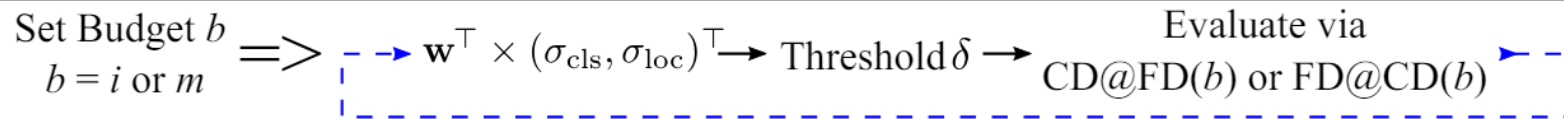


CD: Correct Detection  
 FD: False Detection  
 MD: Missing Detection  
 BG: Background

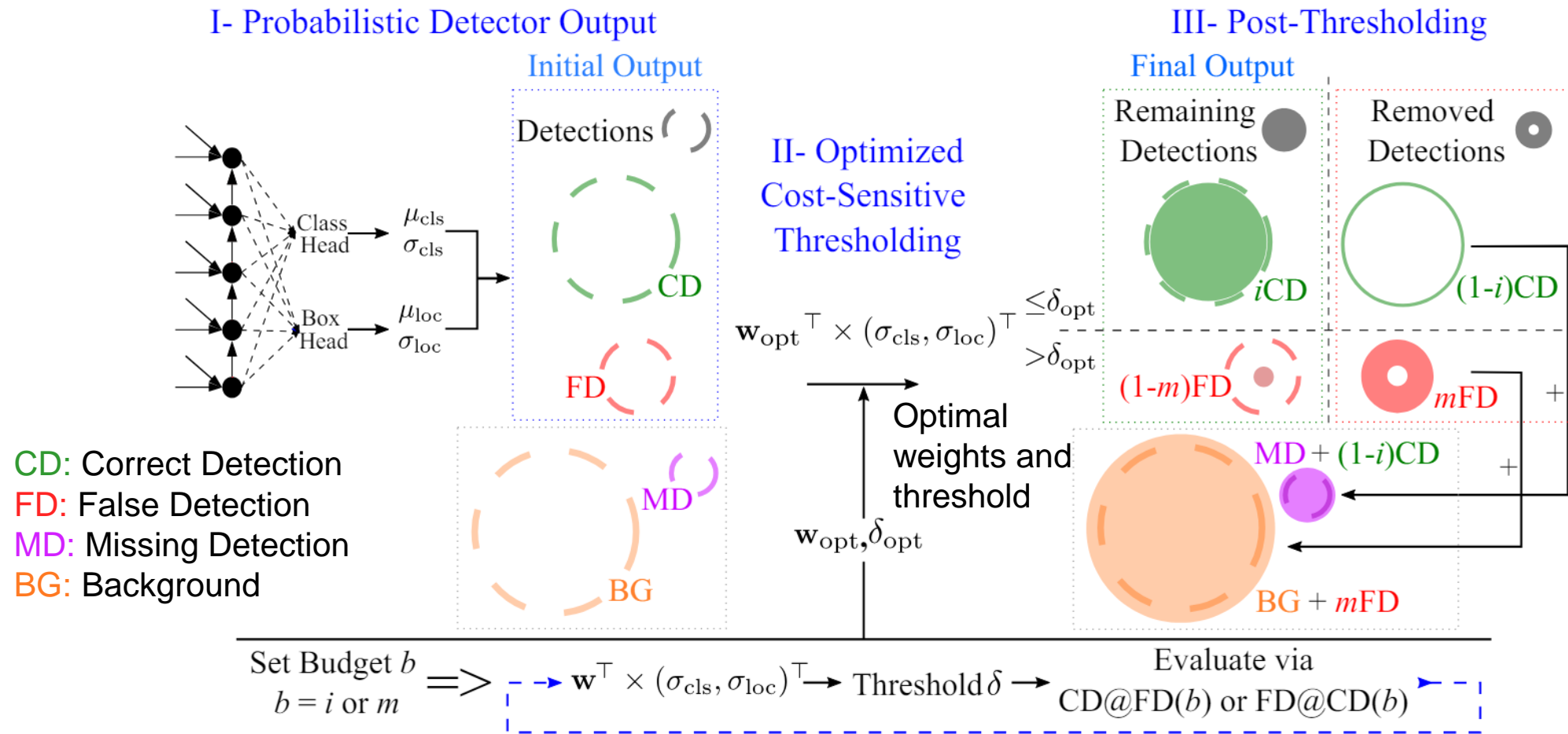
## II- Optimized Cost-Sensitive Thresholding

$$\mathbf{w}_{opt}^T \times (\sigma_{cls}, \sigma_{loc})^T \begin{cases} \leq \delta_{opt} \\ > \delta_{opt} \end{cases}$$

Optimal weights and threshold  
 $\mathbf{w}_{opt}, \delta_{opt}$



# Cost-Sensitive Uncertainty-Based Failure Recognition for Object Detection

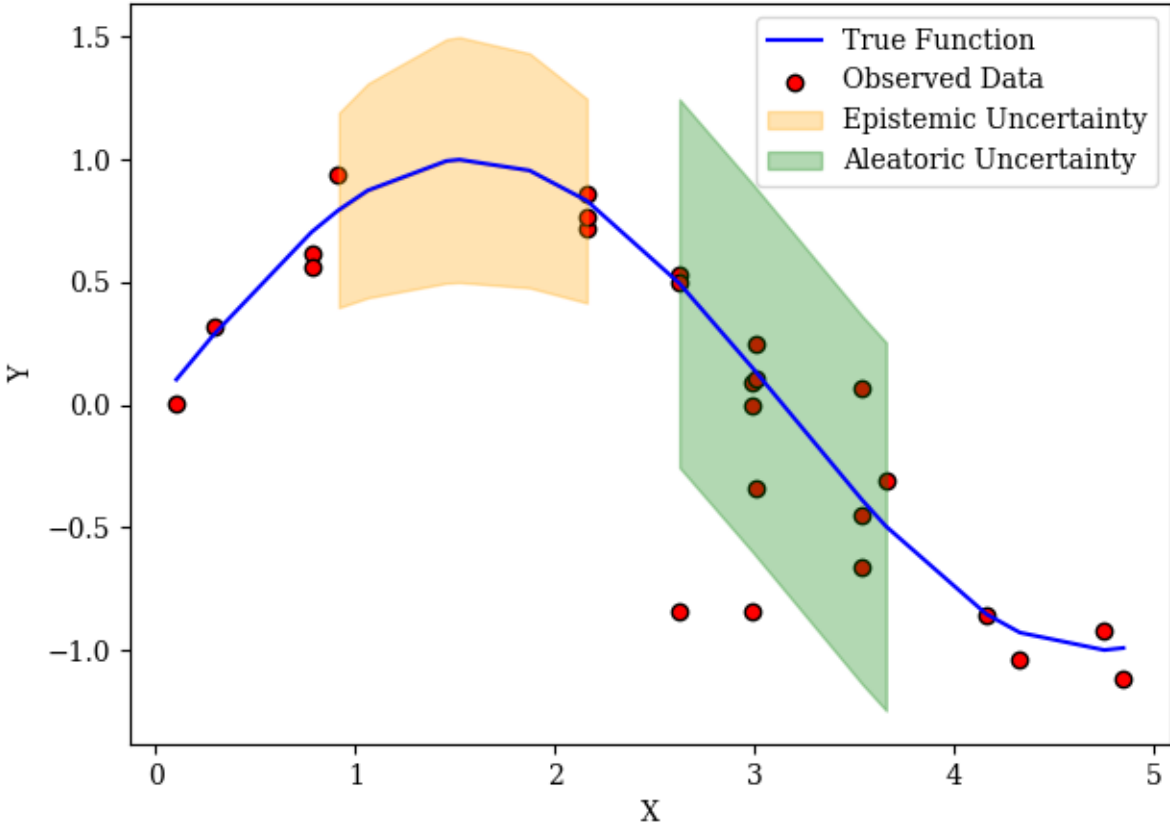




# Uncertainty Estimation

## Classification and Regression – Epistemic and Aleatoric

Epistemic  
Model Uncertainty



Aleatoric  
Data Uncertainty

[3]

# Uncertainty Estimation

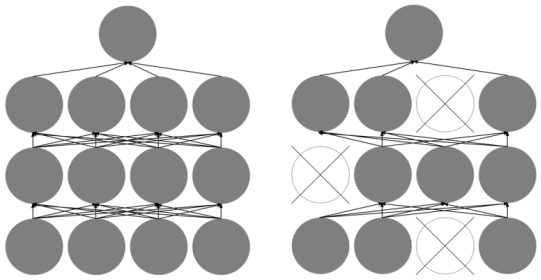
## Classification and Regression – Epistemic and Aleatoric

### Epistemic

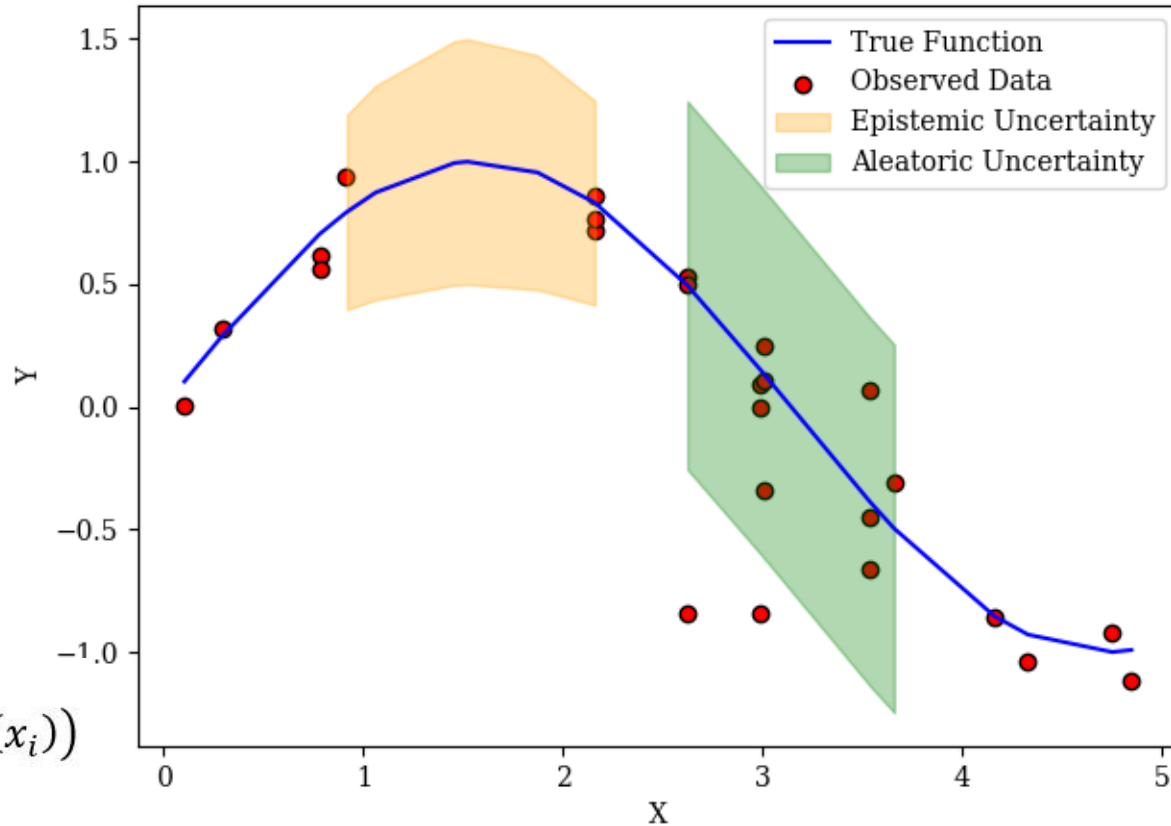
Model Uncertainty

- MC Dropout
- Entropy

Standard    With Dropout



$$H(X) = - \sum_{x_i \in X} P(x_i) * \text{Log}_2(P(x_i))$$



Aleatoric  
Data Uncertainty

# Uncertainty Estimation

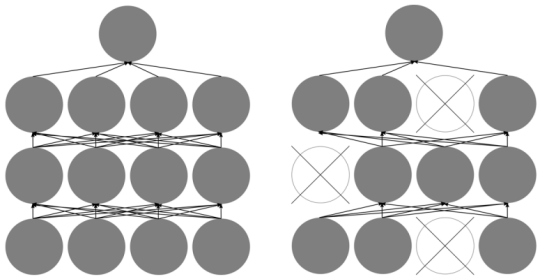
## Classification and Regression – Epistemic and Aleatoric

### Epistemic

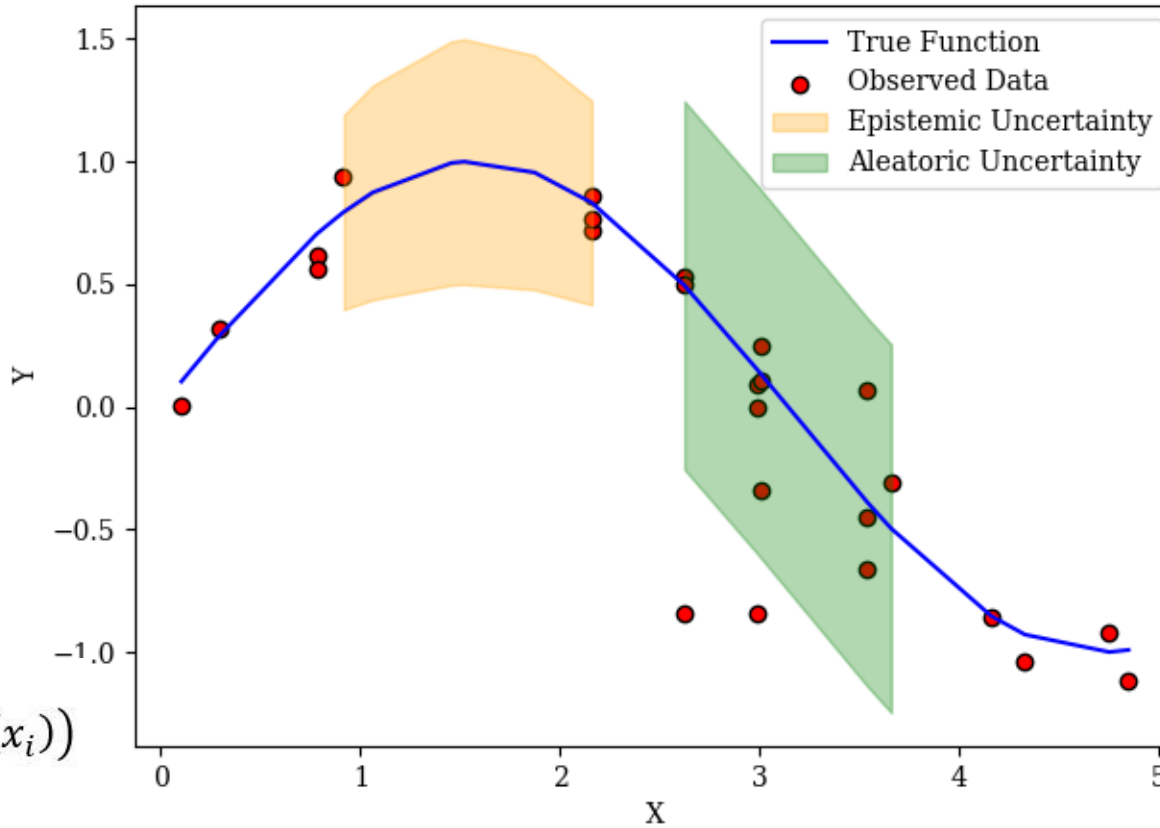
Model Uncertainty

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Standard    With Dropout

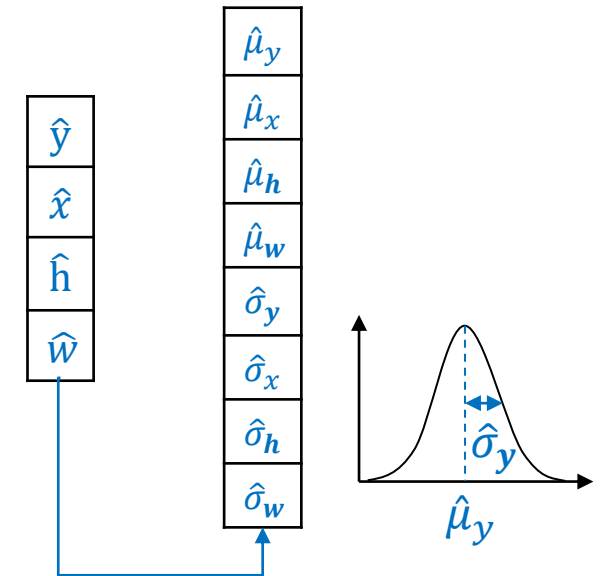


$$H(X) = - \sum_{x_i \in X} P(x_i) * \text{Log}_2(P(x_i))$$



### Aleatoric

Data Uncertainty  
Loss Attenuation



[3,4]

# Datasets

## BDD100K, KITTI and CODA



BDD100K:

- Relatively large
- Many difficult scenarios:
  - Night/crowded images
  - Tiny objects

# Datasets

## BDD100K, KITTI and CODA



### BDD100K:

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- Many difficult scenarios:
  - Night/crowded images
  - Tiny objects

### KITTI:

- Relatively small
- High fidelity dataset with daylight only



# Datasets

## BDD100K, KITTI and CODA



### BDD100K:

- Relatively large
- Many difficult scenarios:
  - Night/crowded images
  - Tiny objects

### KITTI:

- Relatively small
- High fidelity dataset with daylight only



### CODA:

Real-World Road Corner Case Dataset for Object Detection in Autonomous Driving

Evaluation Set

Model pre-trained on BDD100K

[5,6,7]

# Results

## Uncertainty Estimation Methods

**EfficientDet-D0** pre-trained on **COCO**

Input resolution: **1024x512**

Batch size: **8**

**Inference time:**

Baseline: ~35ms

LA: ~30ms

MC: ~185ms

# Results

## Uncertainty Estimation Methods

**EfficientDet-D0** pre-trained on **COCO**

Input resolution: **1024x512**

Batch size: **8**

**Inference time:**

Baseline: ~35ms

LA: ~30ms

MC: ~185ms

**AP**: Average precision

**Acc**: Classification accuracy

**mIoU**: Average intersection over union

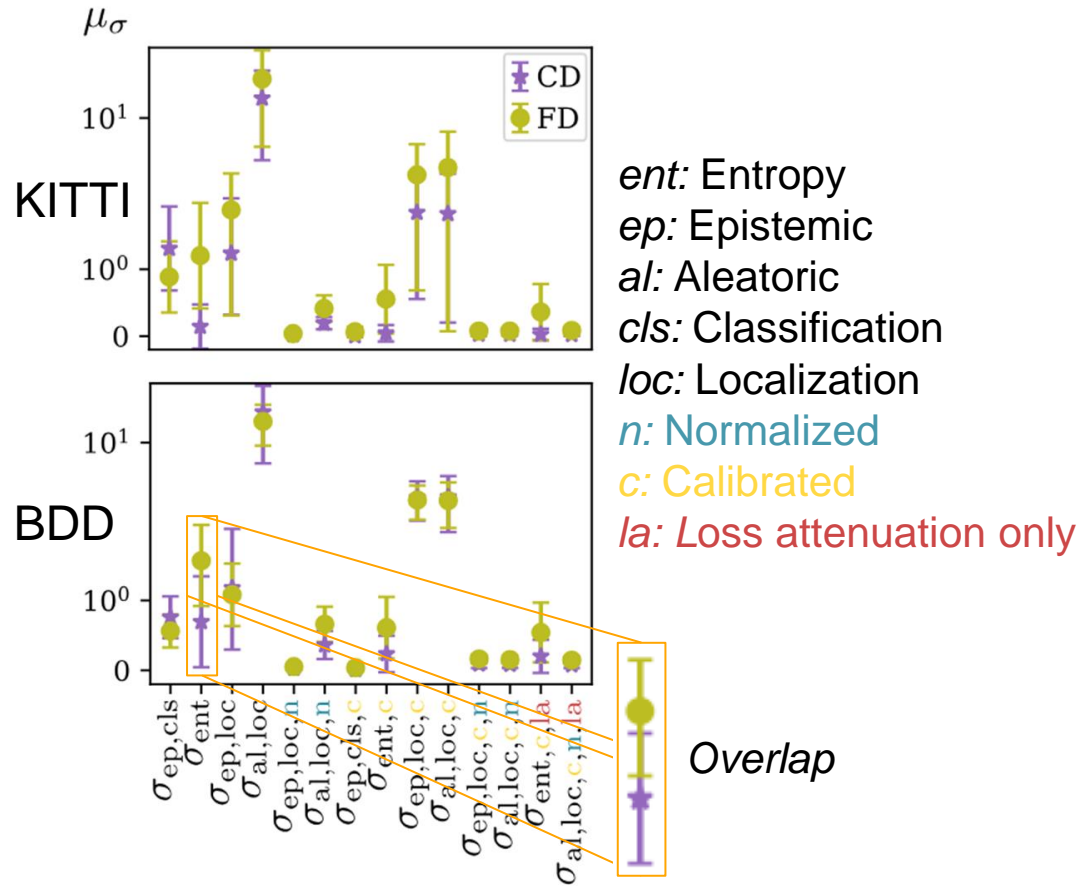
	Method	AP↑	Acc↑	mIoU↑
KITTI	Baseline	72.83±0.12	<b>0.99±0.00</b>	90.06±0.05
	LA	<b>73.26±0.50</b>	<b>0.99±0.00</b>	<b>90.34±0.03</b>
	MC	70.88±0.17	<b>0.99±0.00</b>	89.10±0.02
	MC+LA	70.15±0.09	<b>0.99±0.00</b>	89.03±0.05
BDD	Baseline	24.69±0.09	<b>0.94±0.00</b>	<b>67.74±0.07</b>
	LA	24.38±0.12	<b>0.94±0.00</b>	67.69±0.05
	MC	<b>25.55±0.02</b>	<b>0.94±0.00</b>	67.30±0.02
	MC+LA	24.78±0.01	0.93±0.00	66.60±0.02
CODA	Baseline	16.09±0.07	<b>0.89±0.00</b>	72.23±0.03
	LA	15.53±0.25	<b>0.89±0.00</b>	72.06±0.14
	MC	<b>16.97±0.04</b>	<b>0.89±0.00</b>	<b>73.30±0.08</b>
	MC+LA	16.05±0.25	<b>0.89±0.00</b>	72.19±0.03

- *Correlation between estimation method and dataset characteristics*
- *Better performance than baseline*



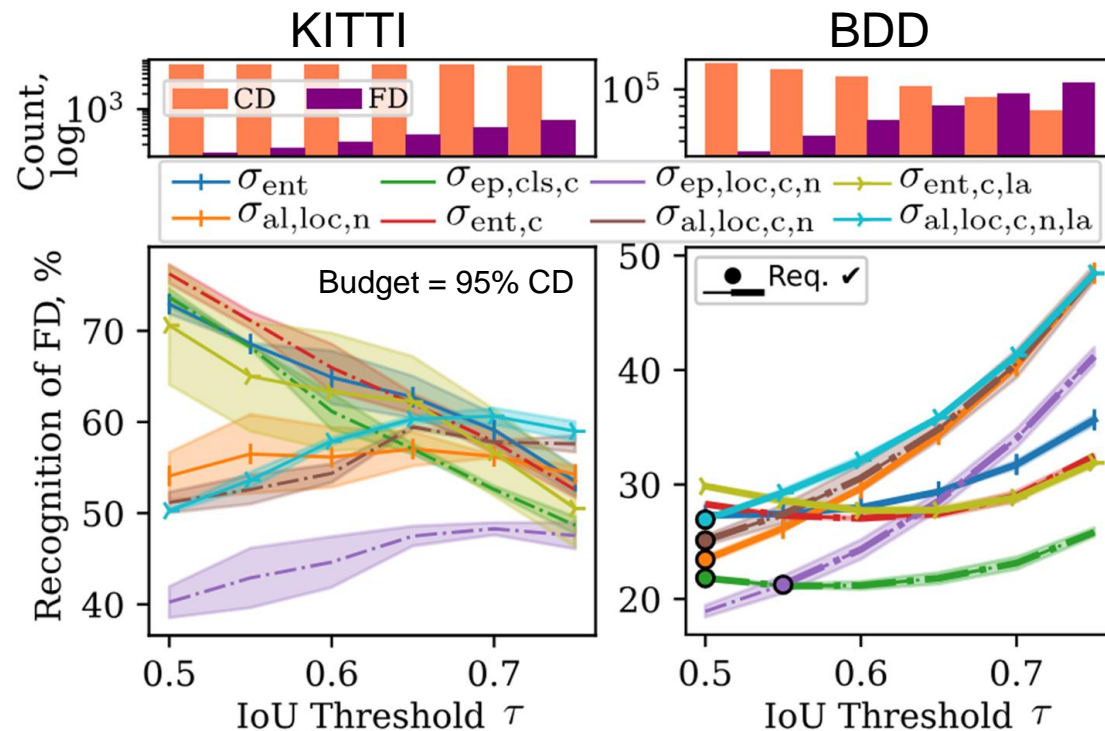
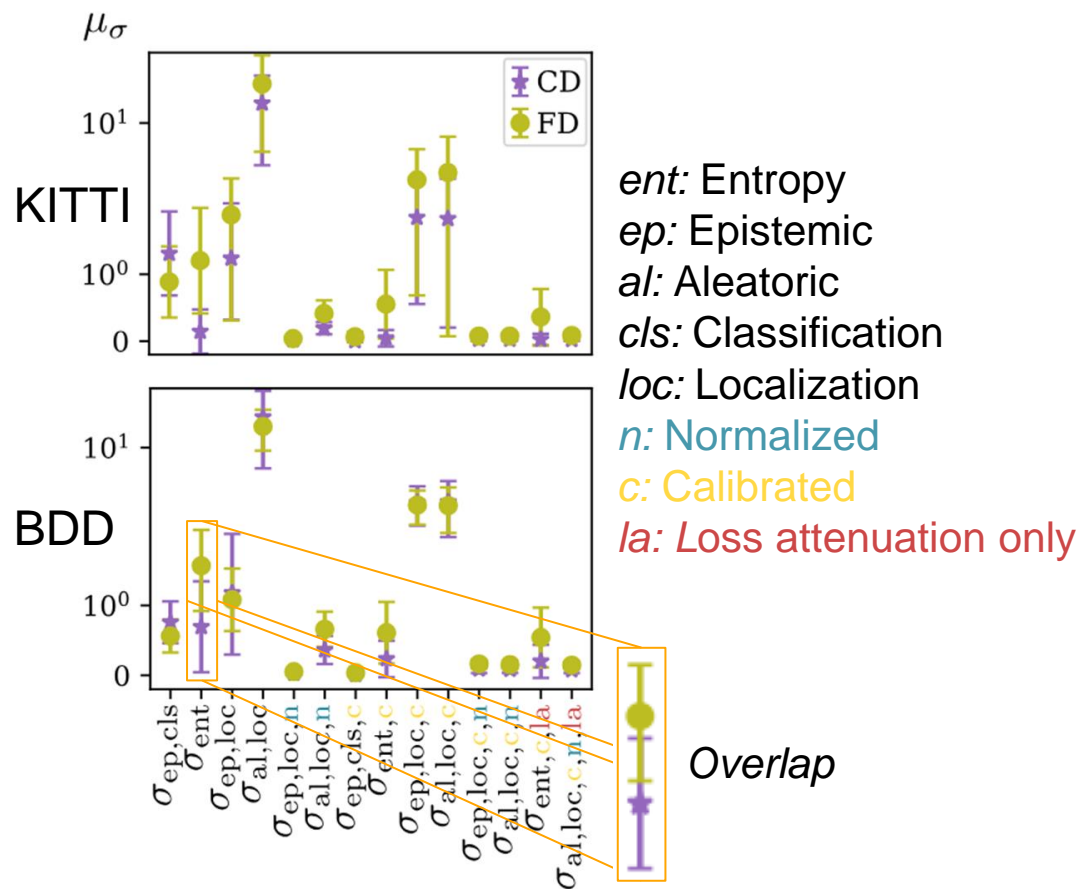
# Results

## Comparison Uncertainty Types



# Results

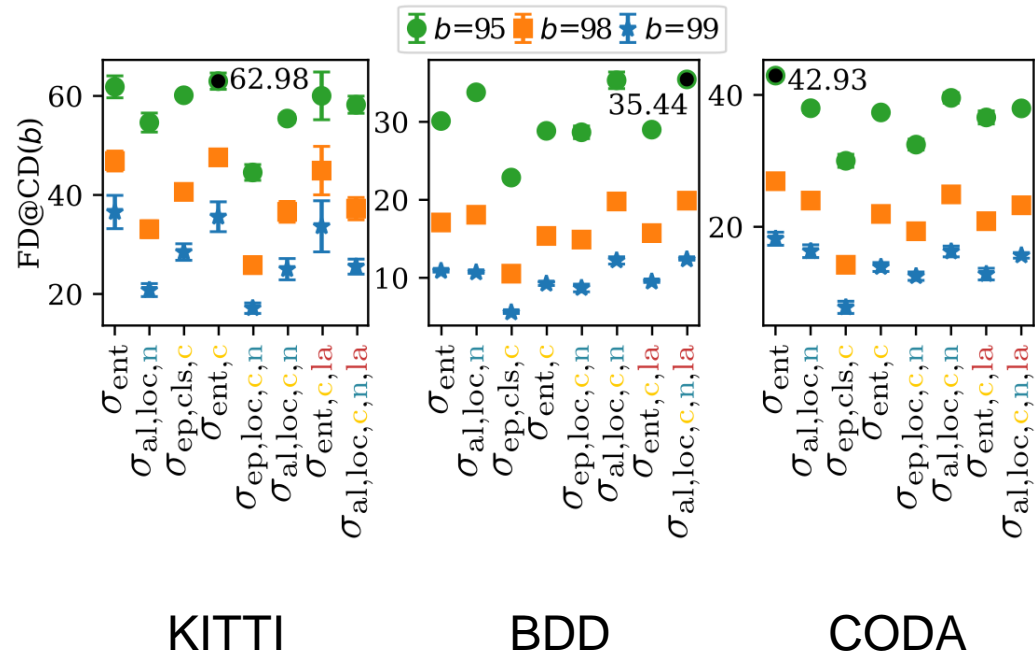
## Comparison Uncertainty Types



- Positive impact of calibration and normalization
- Correlation type vs. IoU Threshold
- Entropy and aleatoric localization uncertainty

# Results

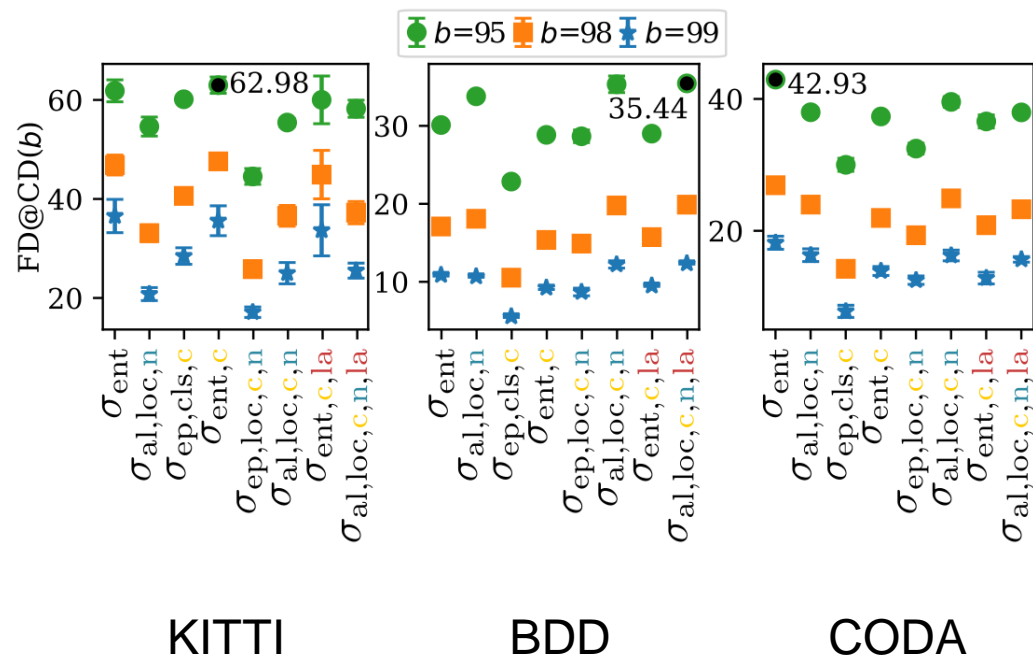
## Budget and Optimization



*Controllable thresholding performance*

# Results

## Budget and Optimization



KITTI

BDD

CODA

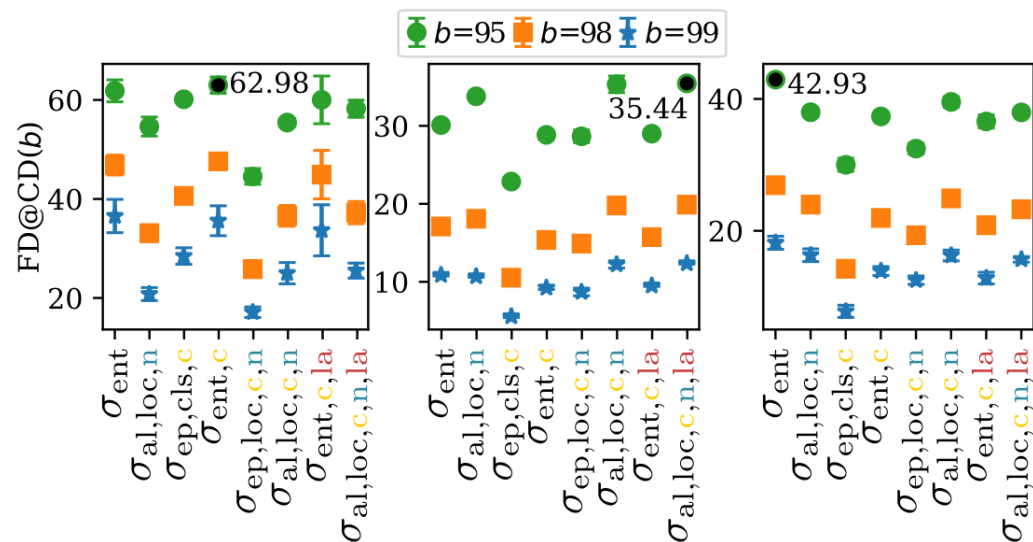
*Controllable thresholding performance*

		Weights			FD@CD95 $\uparrow$	BAcc $\uparrow$
		$\sigma_{ent}$	$\sigma_{ep,loc}$	$\sigma_{al}$		
Standard Sum	$\sum \sigma_{mc+la}$	1.00 $\pm$ 0.00	1.00 $\pm$ 0.00	1.00 $\pm$ 0.00	68.02 $\pm$ 1.97	0.81 $\pm$ 0.01
Optimized Sum	$\sum * \sigma_{mc+la}$	0.16 $\pm$ 0.03	0.03 $\pm$ 0.04	1.0 $\pm$ 0.00	<b>72.36<math>\pm</math>2.72</b>	<b>0.83<math>\pm</math>0.01</b>
KITTI	$\sum \sigma_{la}$	1.00 $\pm$ 0.00	-	1.00 $\pm$ 0.00	65.86 $\pm$ 3.43	0.80 $\pm$ 0.02
	$\sum * \sigma_{la}$	0.14 $\pm$ 0.06	-	0.72 $\pm$ 0.21	<b>70.93<math>\pm</math>1.47</b>	<b>0.83<math>\pm</math>0.01</b>
BDD	$\sum \sigma_{mc+la}$	1.00 $\pm$ 0.00	1.00 $\pm$ 0.00	1.00 $\pm$ 0.00	32.03 $\pm$ 0.24	0.63 $\pm$ 0.00
	$\sum * \sigma_{mc+la}$	0.06 $\pm$ 0.03	0.00 $\pm$ 0.00	0.72 $\pm$ 0.32	<b>37.98<math>\pm</math>0.90</b>	<b>0.67<math>\pm</math>0.00</b>
CODA	$\sum \sigma_{la}$	1.00 $\pm$ 0.00	-	1.00 $\pm$ 0.00	40.60 $\pm$ 0.21	0.68 $\pm$ 0.00
	$\sum * \sigma_{la}$	0.07 $\pm$ 0.02	0.00 $\pm$ 0.00	0.82 $\pm$ 0.25	<b>45.68<math>\pm</math>0.53</b>	<b>0.70<math>\pm</math>0.00</b>
KITTI	$\sum \sigma_{la}$	1.00 $\pm$ 0.00	-	1.00 $\pm$ 0.00	30.65 $\pm$ 0.23	0.63 $\pm$ 0.00
	$\sum * \sigma_{la}$	0.05 $\pm$ 0.02	-	0.72 $\pm$ 0.36	<b>38.11<math>\pm</math>0.21</b>	<b>0.67<math>\pm</math>0.00</b>
BDD	$\sum \sigma_{mc+la}$	1.00 $\pm$ 0.00	1.00 $\pm$ 0.00	1.00 $\pm$ 0.00	32.03 $\pm$ 0.24	0.63 $\pm$ 0.00
	$\sum * \sigma_{mc+la}$	0.06 $\pm$ 0.03	0.00 $\pm$ 0.00	0.72 $\pm$ 0.32	<b>37.98<math>\pm</math>0.90</b>	<b>0.67<math>\pm</math>0.00</b>
CODA	$\sum \sigma_{la}$	1.00 $\pm$ 0.00	-	1.00 $\pm$ 0.00	38.49 $\pm$ 0.96	0.67 $\pm$ 0.00
	$\sum * \sigma_{la}$	0.10 $\pm$ 0.01	-	0.99 $\pm$ 0.00	<b>43.95<math>\pm</math>0.43</b>	<b>0.69<math>\pm</math>0.00</b>

*Using only entropy and aleatoric uncertainty:*

# Results

## Budget and Optimization



KITTI

BDD

CODA

*Controllable thresholding performance*

		Weights			FD@CD95 $\uparrow$	BAcc $\uparrow$
		$\sigma_{ent}$	$\sigma_{ep,loc}$	$\sigma_{al}$		
Standard Sum	$\sum \sigma_{mc+la}$	1.00 $\pm$ 0.00	1.00 $\pm$ 0.00	1.00 $\pm$ 0.00	68.02 $\pm$ 1.97	0.81 $\pm$ 0.01
Optimized Sum	$\sum * \sigma_{mc+la}$	0.16 $\pm$ 0.03	0.03 $\pm$ 0.04	1.0 $\pm$ 0.00	<b>72.36<math>\pm</math>2.72</b>	<b>0.83<math>\pm</math>0.01</b>
KITTI	$\sum \sigma_{la}$	1.00 $\pm$ 0.00	-	1.00 $\pm$ 0.00	65.86 $\pm$ 3.43	0.80 $\pm$ 0.02
	$\sum * \sigma_{la}$	0.14 $\pm$ 0.06	-	0.72 $\pm$ 0.21	<b>70.93<math>\pm</math>1.47</b>	<b>0.83<math>\pm</math>0.01</b>
BDD	$\sum \sigma_{mc+la}$	1.00 $\pm$ 0.00	1.00 $\pm$ 0.00	1.00 $\pm$ 0.00	32.03 $\pm$ 0.24	0.63 $\pm$ 0.00
	$\sum * \sigma_{mc+la}$	0.06 $\pm$ 0.03	0.00 $\pm$ 0.00	0.72 $\pm$ 0.32	<b>37.98<math>\pm</math>0.90</b>	<b>0.67<math>\pm</math>0.00</b>
CODA	$\sum \sigma_{la}$	1.00 $\pm$ 0.00	-	1.00 $\pm$ 0.00	30.65 $\pm$ 0.23	0.63 $\pm$ 0.00
	$\sum * \sigma_{la}$	0.05 $\pm$ 0.02	-	0.72 $\pm$ 0.36	<b>38.11<math>\pm</math>0.21</b>	<b>0.67<math>\pm</math>0.00</b>
KITTI	$\sum \sigma_{mc+la}$	1.00 $\pm$ 0.00	1.00 $\pm$ 0.00	1.00 $\pm$ 0.00	40.60 $\pm$ 0.21	0.68 $\pm$ 0.00
	$\sum * \sigma_{mc+la}$	0.07 $\pm$ 0.02	0.00 $\pm$ 0.00	0.82 $\pm$ 0.25	<b>45.68<math>\pm</math>0.53</b>	<b>0.70<math>\pm</math>0.00</b>
BDD	$\sum \sigma_{la}$	1.00 $\pm$ 0.00	-	1.00 $\pm$ 0.00	38.49 $\pm$ 0.96	0.67 $\pm$ 0.00
	$\sum * \sigma_{la}$	0.10 $\pm$ 0.01	-	0.99 $\pm$ 0.00	<b>43.95<math>\pm</math>0.43</b>	<b>0.69<math>\pm</math>0.00</b>

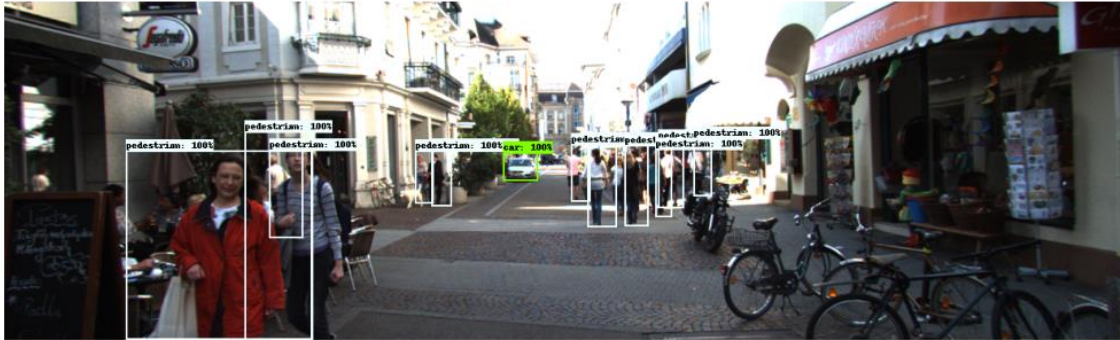
*Using only entropy and aleatoric uncertainty:*

- +2–11% via optimized combination
- +36–60% over conventional methods

# Results

## Qualitative – Failure Recognition and Auto-Labeling

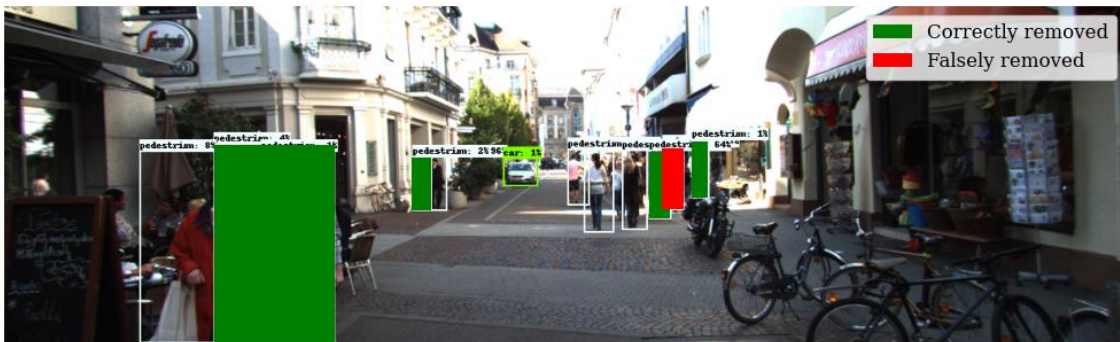
Ground Truth



## Failure Recognition

Post-Thresholding

Eval on IoU 0.75



# Results

## Qualitative – Failure Recognition and Auto-Labeling

Ground Truth



## Failure Recognition

Post-Thresholding

Eval on IoU 0.75



# Results

## Qualitative – Failure Recognition and Auto-Labeling

Ground Truth



## Failure Recognition

Post-Thresholding

Eval on IoU 0.75

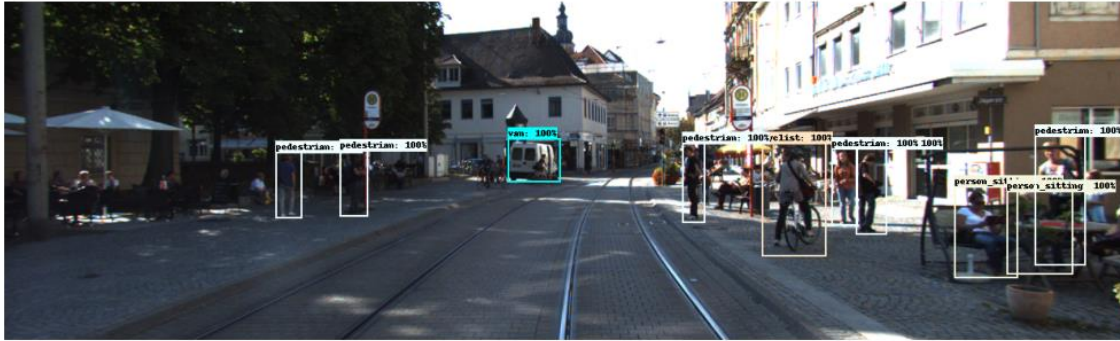




# Results

## Qualitative – Failure Recognition and Auto-Labeling

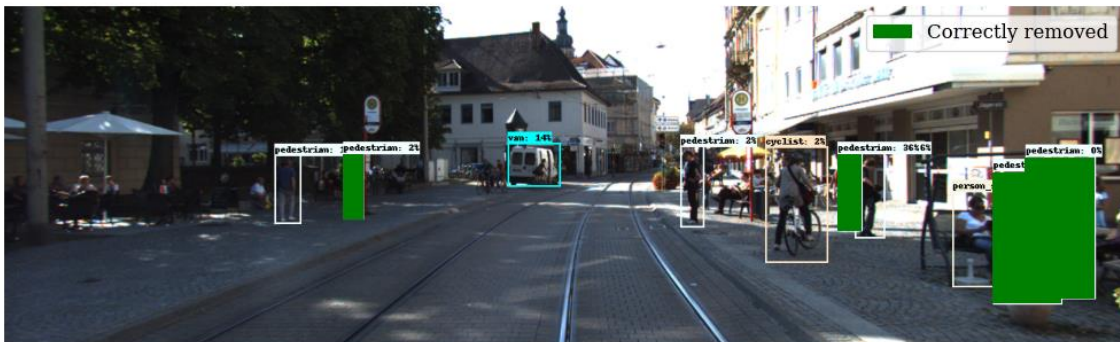
Ground Truth



## Failure Recognition

Post-Thresholding

Eval on IoU 0.75



# Results

## Qualitative – Failure Recognition and Auto-Labeling

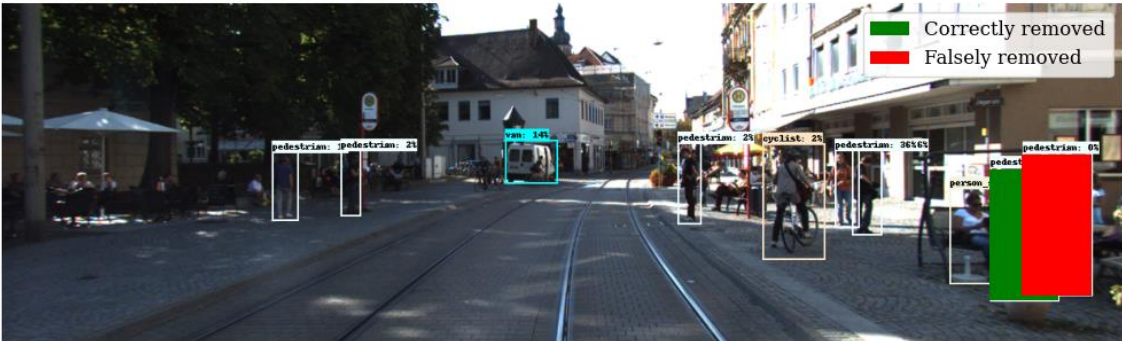
Ground Truth



### Failure Recognition

Post-Thresholding

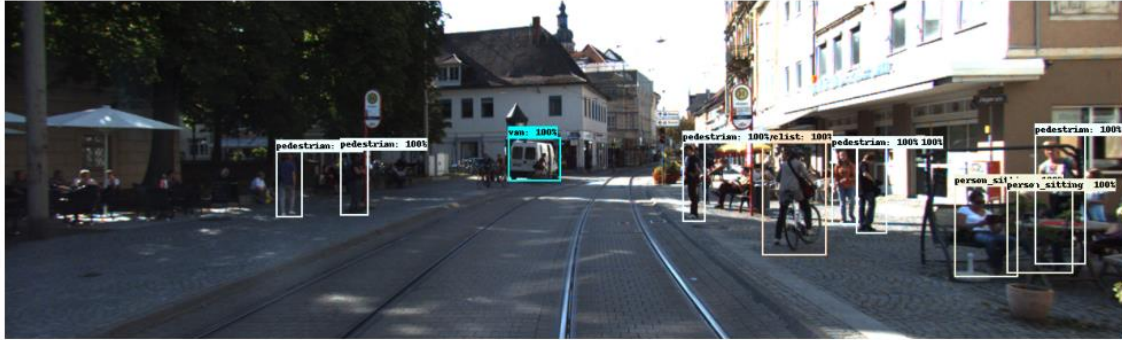
Eval on IoU 0.50



# Results

## Qualitative – Failure Recognition and Auto-Labeling

Ground Truth



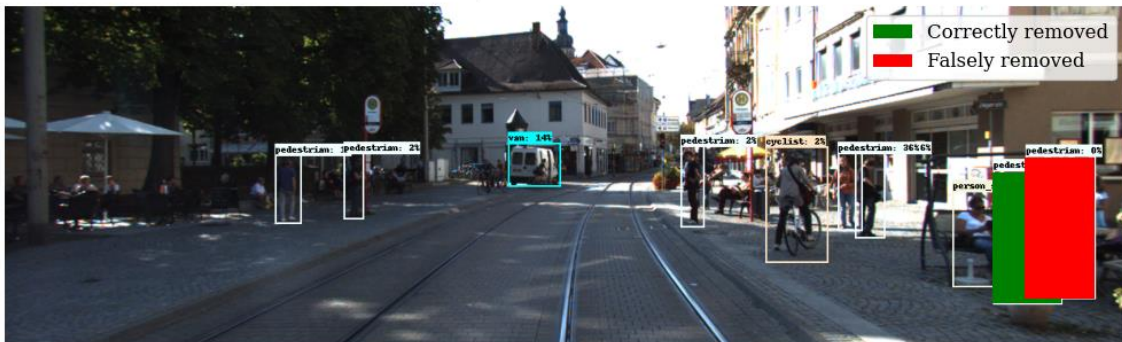
Ground Truth



## Failure Recognition

Post-Thresholding

Eval on IoU 0.50



## Auto-Labeling

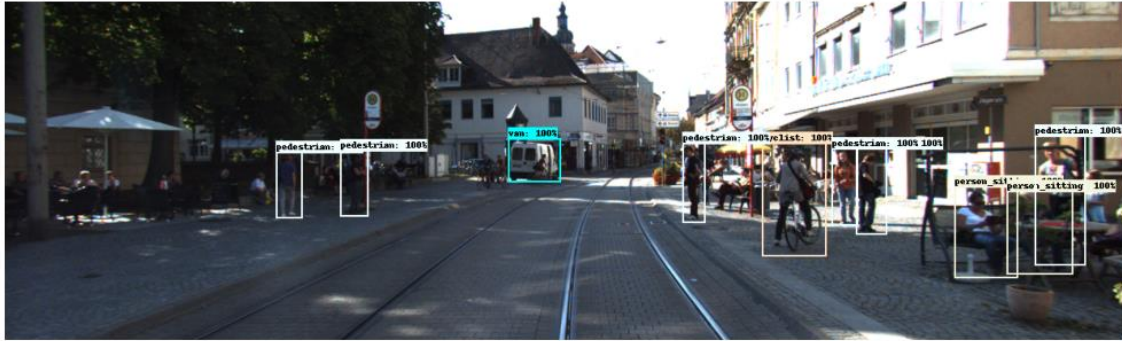
Post-Thresholding



# Results

## Qualitative – Failure Recognition and Auto-Labeling

Ground Truth



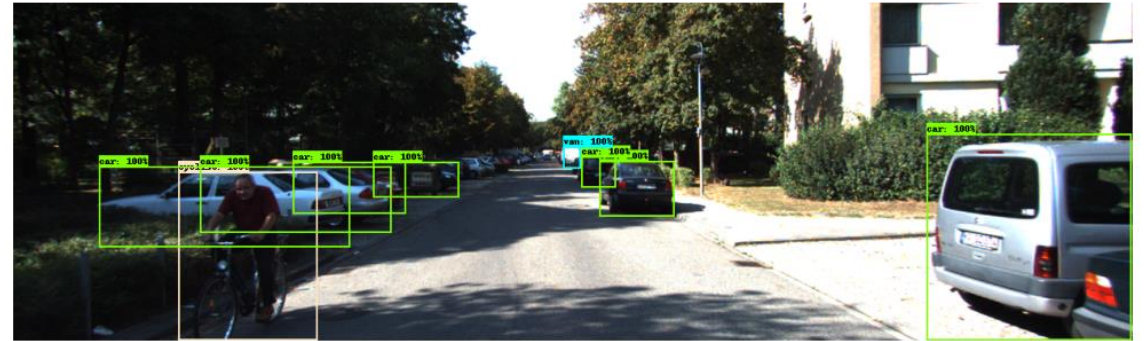
### Failure Recognition

Post-Thresholding



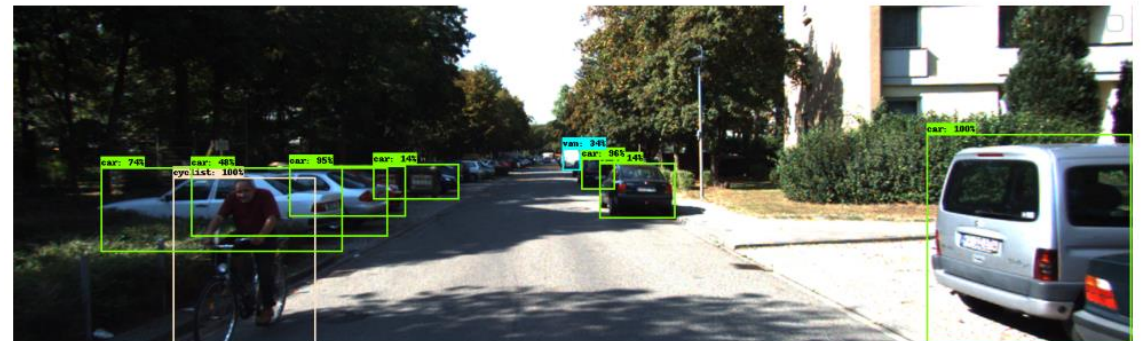
Eval on IoU 0.50

Ground Truth



### Auto-Labeling

Post-Thresholding



# Summary

In this work, we:

- › **Define cost-sensitivity** for object detection
- › **Automate** the thresholding process
- › **Investigate** and **Optimize** the combination of different uncertainties
- › **Introduce metrics** and **requirements**

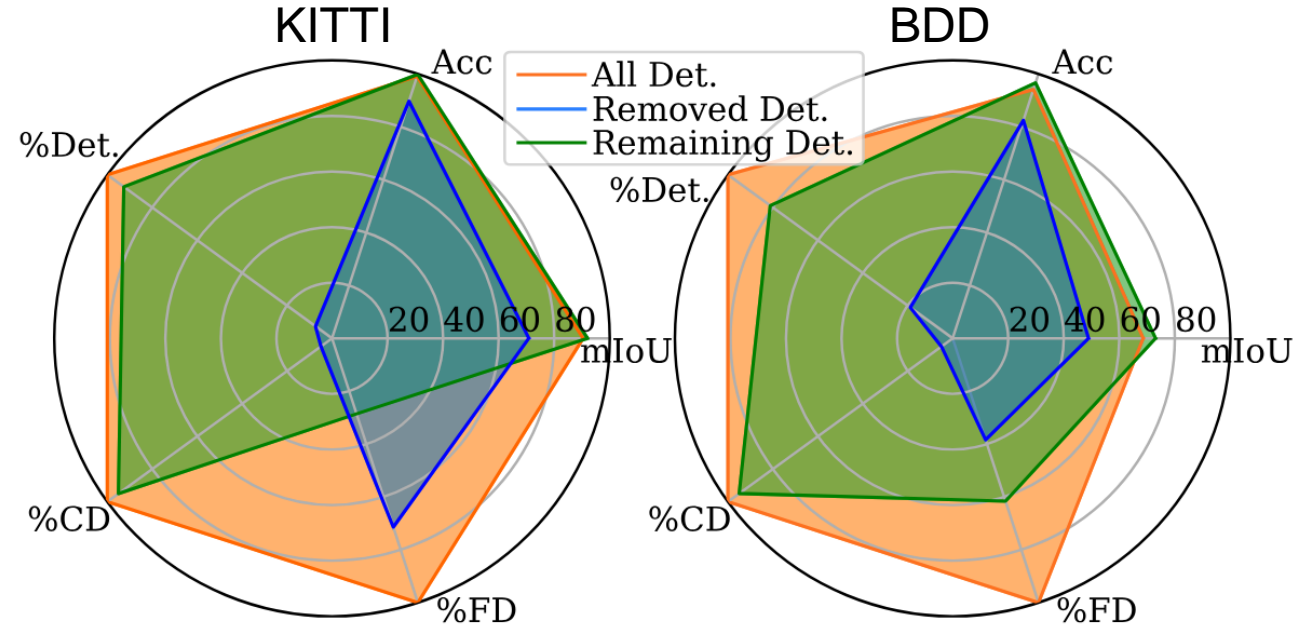
Paper #176



# Summary

In this work, we:

- › **Define cost-sensitivity** for object detection
- › **Automate** the thresholding process
- › **Investigate** and **Optimize** the combination of different uncertainties
- › **Introduce metrics and requirements**



Key advantages:

- › **Model-Agnostic** Failure Recognition
- › **Application-Agnostic** Budget-Based Thresholding
- › **Efficient Uncertainty Estimation** via Loss Attenuation
- › **Minimal Model Expansion** with 0.07% Increase in Parameters
- › **Considerable Decrease in False Detections Enhancing Overall Performance**

Paper #176



# Appendix

# References

1. Moussa Kassem Sbeyti, Michelle Karg, Christian Wirth, Azarm Nowzad, and Sahin Albayrak. Overcoming the limitations of localization uncertainty: Efficient and exact non-linear post-processing and calibration. In Machine Learning and Knowledge Discovery in Databases: Research Track. ECML PKDD 2023., pages 52–68. Springer Nature Switzerland, 2023.
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3. Alex Kendall and Yarin Gal. What uncertainties do we need in bayesian deep learning for computer vision? Advances in Neural Information Processing Systems, 30, 2017.
4. Yarin Gal and Zoubin Ghahramani. Dropout as a Bayesian approximation: Representing model uncertainty in deep learning. In 33rd International Conference on Machine Learning, pages 1050–1059, 2016.
5. Andreas Geiger, Philip Lenz, and Raquel Urtasun. Are we ready for autonomous driving? The kitti vision benchmark suite. In IEEE/CVF Conference on Computer Vision and Pattern Recognition, pages 3354–3361, 2012.
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7. Fisher Yu, Haofeng Chen, Xin Wang, Wenqi Xian, Yingying Chen, Fangchen Liu, Vashisht Madhavan, and Trevor Darrell. Bdd100k: A diverse driving dataset for heterogeneous multitask learning. In IEEE/CVF Conference on Computer Vision and Pattern Recognition, pages 2633–2642, 2020.



# Uncertainty Estimation

## Classification and Regression – Epistemic

### Monte Carlo Dropout

Dropout on during Training

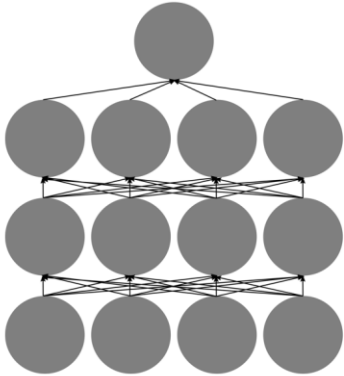


Dropout on during Inference

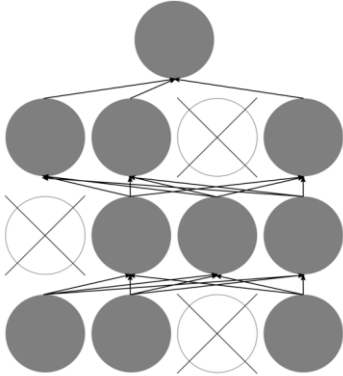


Sample during Inference

Standard Network



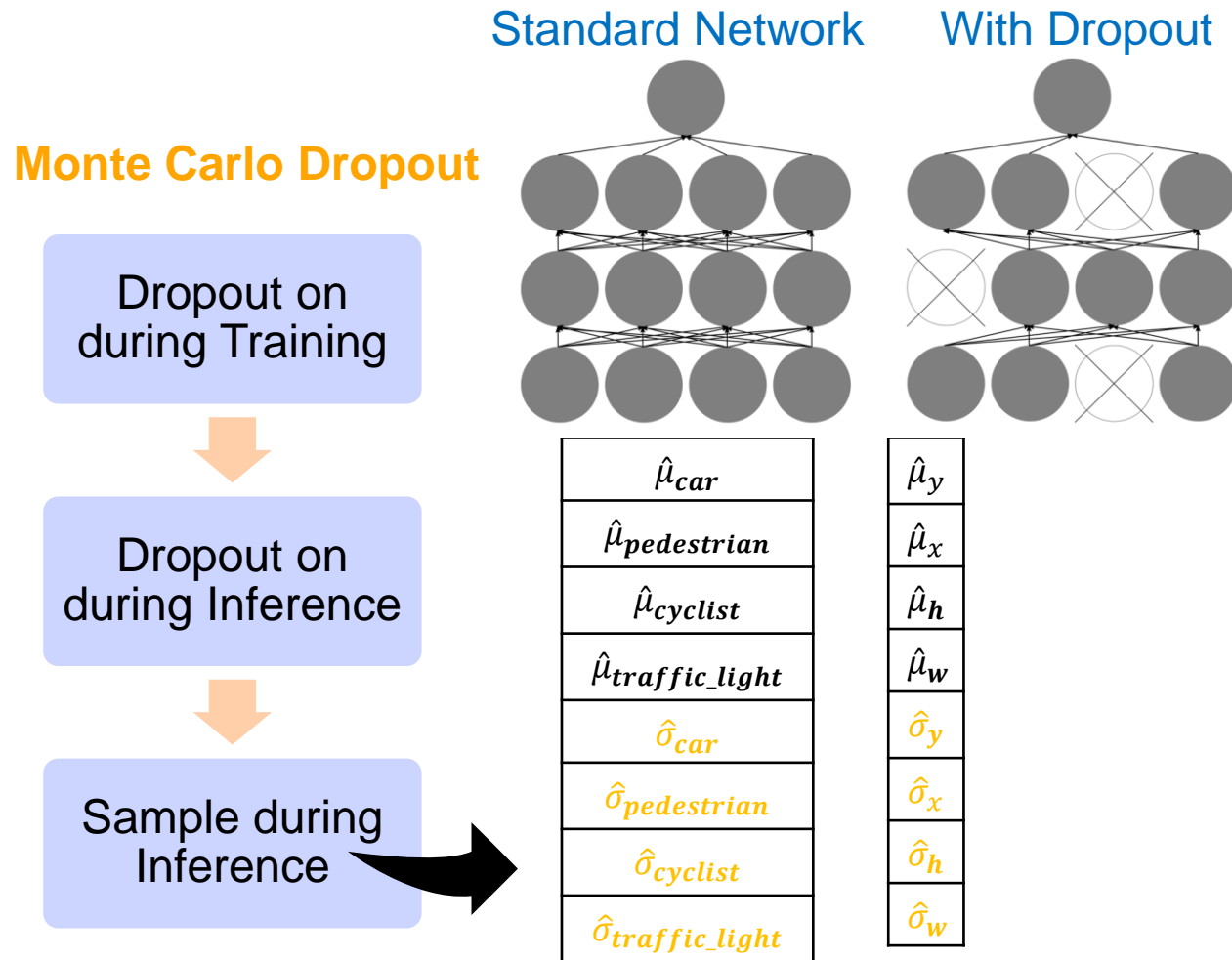
With Dropout



[4]

# Uncertainty Estimation

## Classification and Regression – Epistemic



[4]

# Uncertainty Estimation

## Classification and Regression – Epistemic

### Monte Carlo Dropout

Dropout on during Training

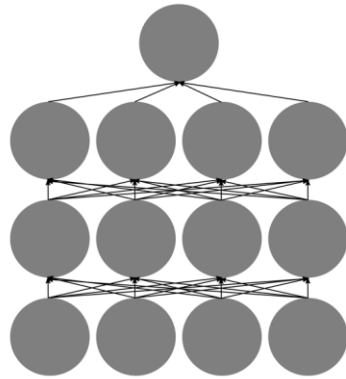


Dropout on during Inference



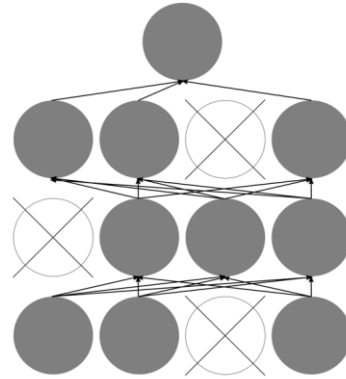
Sample during Inference

Standard Network



$\hat{\mu}_{car}$
$\hat{\mu}_{pedestrian}$
$\hat{\mu}_{cyclist}$
$\hat{\mu}_{traffic\_light}$
$\hat{\sigma}_{car}$
$\hat{\sigma}_{pedestrian}$
$\hat{\sigma}_{cyclist}$
$\hat{\sigma}_{traffic\_light}$

With Dropout



$\hat{\mu}_y$
$\hat{\mu}_x$
$\hat{\mu}_h$
$\hat{\mu}_w$
$\hat{\sigma}_y$
$\hat{\sigma}_x$
$\hat{\sigma}_h$
$\hat{\sigma}_w$

**Entropy** represents the separation capabilities of the model between the classes

$$H(X) = - \sum_{x_i \in X} P(x_i) * \text{Log}_2(P(x_i))$$

Cat	0.8	0.2	0.3
Dog	0.1	0.5	0.4
Goat	0.1	0.3	0.3
	Low	Medium	High

[4]

# Uncertainty Estimation

## Regression – Aleatoric

Observation noise,  
weather conditions,  
misleading situations

# Input

# Uncertainty Estimation

## Regression – Aleatoric

Observation noise,  
weather conditions,  
misleading situations

Input → Network

Rewrite box loss with loss  
attenuation

Negative log-likelihood  $\mathcal{L}_{\text{NN}} = \frac{1}{2N} \sum_{i=1}^N \frac{\|y_i^* - f(x_i)\|^2}{\sigma(x_i)^2} + \log \sigma(x_i)^2$

# Uncertainty Estimation

## Regression – Aleatoric

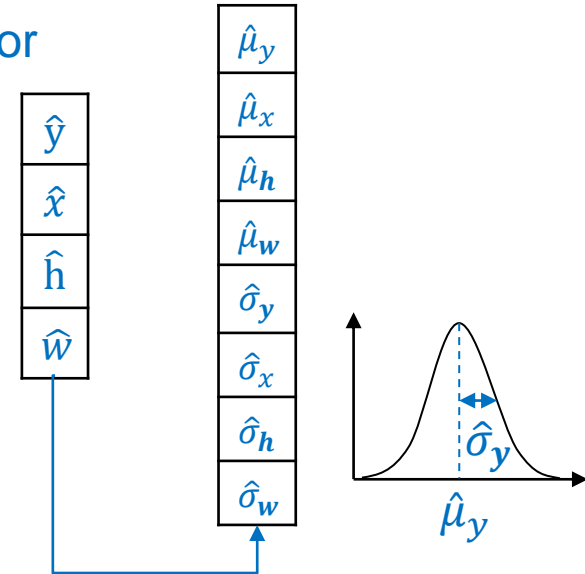
Observation noise,  
weather conditions,  
misleading situations

Extend output to 8  
values per anchor

Input → Network → Output

Rewrite box loss with loss  
attenuation

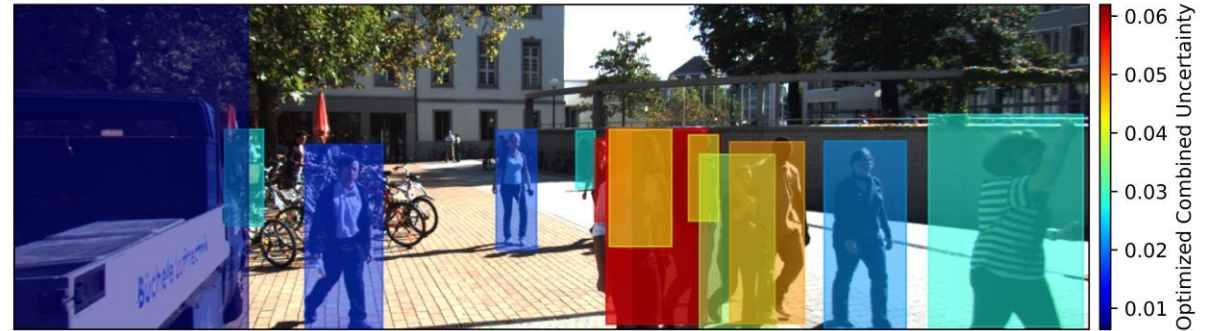
Negative log-likelihood  $\mathcal{L}_{\text{NN}} = \frac{1}{2N} \sum_{i=1}^N \frac{\|y_i^* - f(x_i)\|^2}{\sigma(x_i)^2} + \log \sigma(x_i)^2$



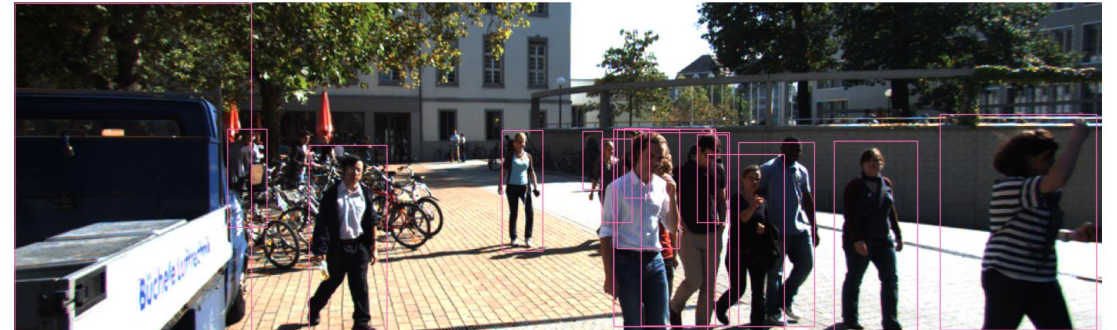
*The uncertainty is learned as a function of the data*

# Results

## Example



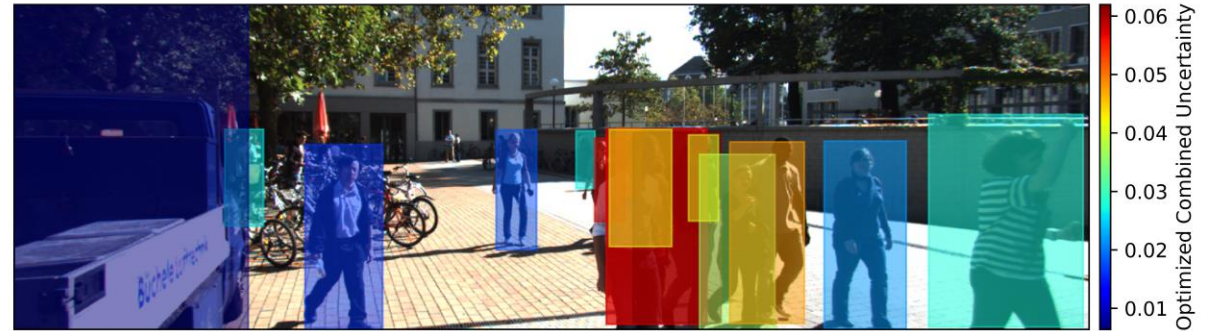
Pre-thresholding



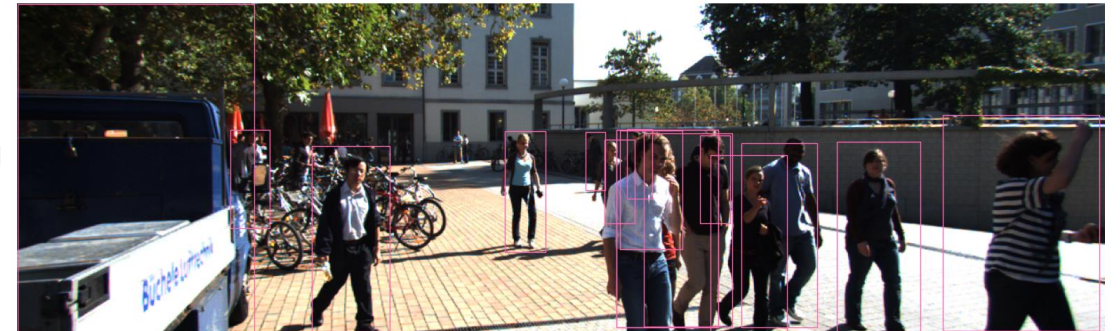
# Results

## Example

**Optimal Threshold = 0.028**  
Optimization for a budget of  
95% CDs over the IoU  
thresholds 0.5-0.75



Pre-  
thresholding





# Results

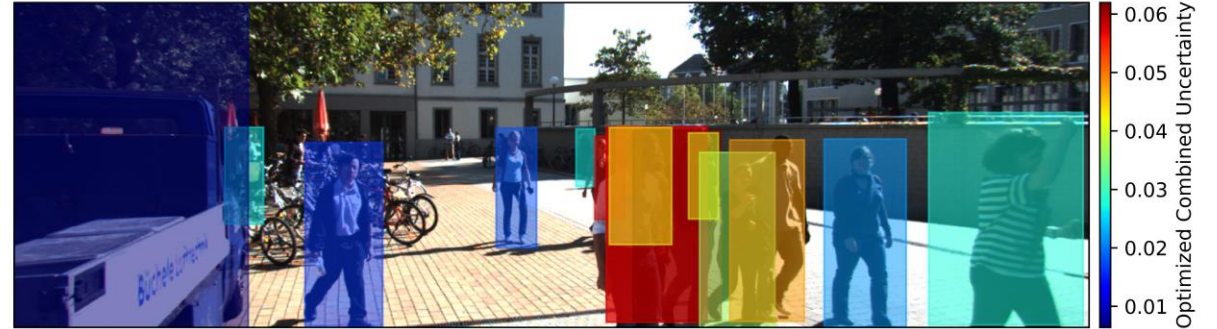
## Example

**Optimal Threshold = 0.028**  
Optimization for a budget of  
95% CDs over the IoU  
thresholds 0.5-0.75

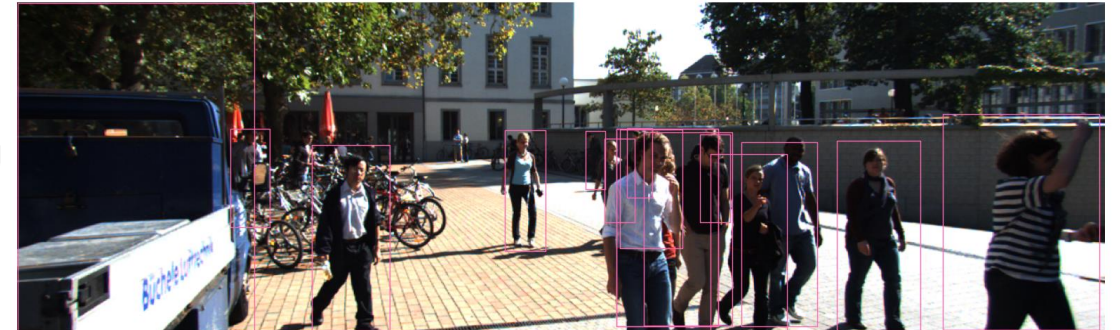


All classes correct

#	IoU
1	0.66
2	0.70
3	0.77
4	0.66
5	0.59
6	0.73
7	0.63
8	0.77
9	0.69
10	0.93
11	0.88
12	0.78
13	0.54
14	0.83
15	0.36
16	0.99



Pre-  
thresholding



# Results

## Example

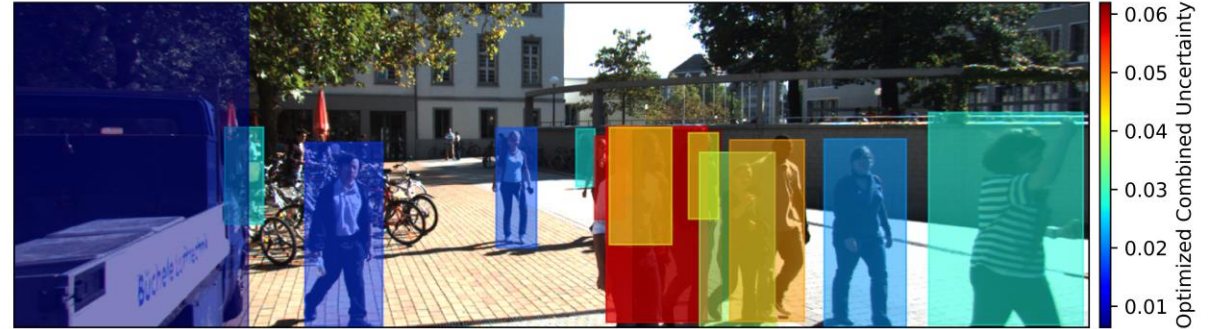
**Optimal Threshold = 0.028**  
 Optimization for a budget of 95% CDs over the IoU thresholds 0.5-0.75



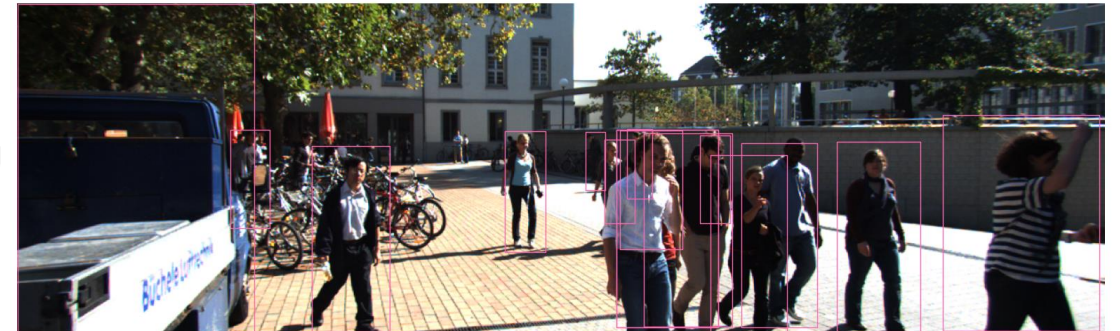
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9	0.69
10	0.93
11	0.88
12	0.78
13	0.54
14	0.83
15	0.36
16	0.99

Removed



Pre-thresholding



Post-thresholding

